Quiz 4

EECS 203 Spring 2016

Name (Print):
uniqname (Print):
Instructions. You have <u>25</u> minutes to complete this quiz. You may not use any sources of information, including electronic devices, textbooks, or notes. Leave at least one seat between yourself and other students. Please write clearly. If we cannot read your writing, it will not be graded.
Honor Code. This course operates under the rules of the College of Engineering Honor Code. Your signature endorses the pledge below. After you finish your exam, please sign on the line below:
I have neither given nor received aid on this examination, nor have I concealed any violations of the Honor Code.

1. Recall the following from our text: [10 points]

RSA Decryption

The plaintext message can be quickly recovered from a ciphertext message when the decryption key d, an inverse of e modulo (p-1)(q-1), is known. [Such an inverse exists because gcd(e, (p-1)(q-1)) = 1.] To see this, note that if $de \equiv 1 \pmod{(p-1)(q-1)}$, there is an integer k such that de = 1 + k(p-1)(q-1). It follows that

$$C^d \equiv (M^e)^d = M^{de} = M^{1+k(p-1)(q-1)} \pmod{n}.$$

By Fermat's little theorem [assuming that gcd(M, p) = gcd(M, q) = 1, which holds except in rare cases, which we cover in Exercise 28], it follows that $M^{p-1} \equiv 1 \pmod{p}$ and $M^{q-1} \equiv 1 \pmod{q}$. Consequently,

$$C^d \equiv M \cdot (M^{p-1})^{k(q-1)} \equiv M \cdot 1 = M \pmod{p}$$

and

$$C^d \equiv M \cdot (M^{q-1})^{k(p-1)} \equiv M \cdot 1 = M \pmod{q}.$$

Because gcd(p, q) = 1, it follows by the Chinese remainder theorem that

$$C^d \equiv M \pmod{pq}$$
.

a. If e=3, p=2 and q=5, what is the decryption key, "d"? Briefly explain/justify your answer. [5]

b. If the cyphertext is 6, what is the plaintext? Use your answer from "a" above—you will get credit if you do this part correctly even if your value of "d" is incorrect. Again, you must briefly show your work. [5]

2)	 How many bit strings of length 6 have <u>at least</u> one of the following properties: Start "010" Start with "11"
	• End in a "00" You are to give your answer as a number and show your work. To have a chance at partial credit, it must be clear exactly what you did. [8 points]
3)	How many <u>6</u> -card poker hands consist of exactly 2 pairs? That is two of one rank of card, two of another rank of card, one of a third rank, and one of a forth rank of card? Recall that a deck of cards consists of 4 suits each with one card of each of the 13 ranks. <u>You should leave your answer as an equation</u> . <i>Again, notice we are talking about a <u>six</u>-card poker hand</i> . [8 points]
4)	How many bit strings of length 19 contain at least 9 1's and at least 9 0's? You may leave your
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