

**University of Michigan**  
**EECS 311: Electronic Circuits**  
**Fall 2009**

Quiz 2

11/18/2009

NAME: \_\_\_\_\_

**Honor Code:**

I have neither given nor received unauthorized aid on this examination, nor have I concealed any violations of the Honor Code.

Signature \_\_\_\_\_

Problem	Points	Score	Initials
1	20		
2	25		
3	30		
4	25		
	Total		

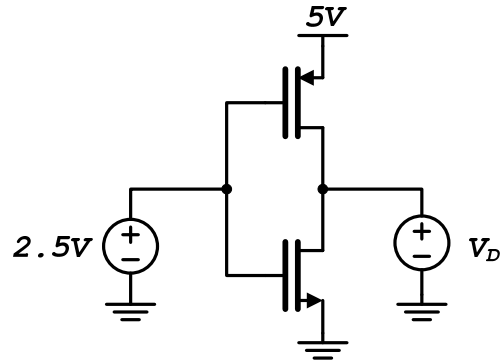


**Problem 1 (20 Points):** Potpourri.

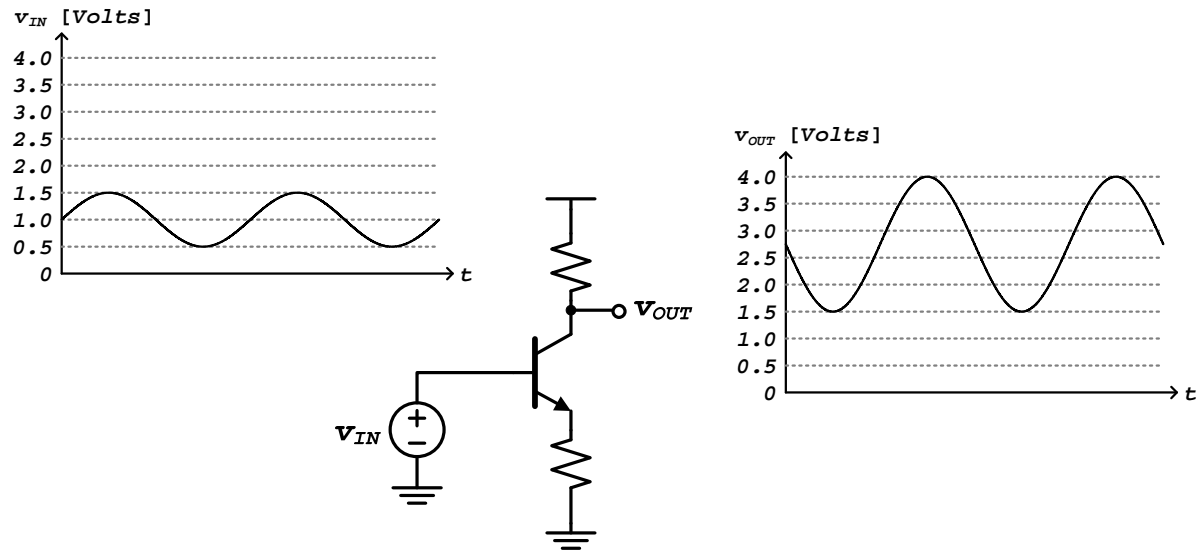
- a) For the circuit below, find the range of  $V_D$  that will simultaneously bias the NMOS and PMOS in the Saturation region.

$$V_{tn} = 1V$$

$$V_{tp} = -1V$$



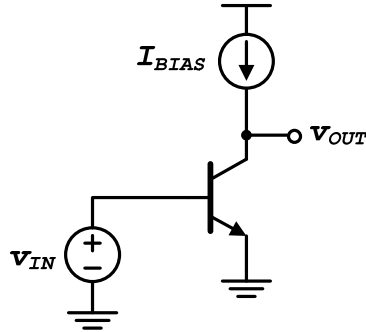
- b) Determine the values of the DC and ac components of the waveforms shown below, assuming the signal are sinusoidal with frequency  $\omega = \omega_0$ . Additionally, evaluate the ac gain  $a_v = v_{out}/v_{in}$  of the circuit.



Total	=	DC Component	+	ac Component
$v_{IN}$	=	_____	+	_____
$v_{OUT}$	=	_____	+	_____
ac Gain $a_v = v_{out}/v_{in} =$ _____				

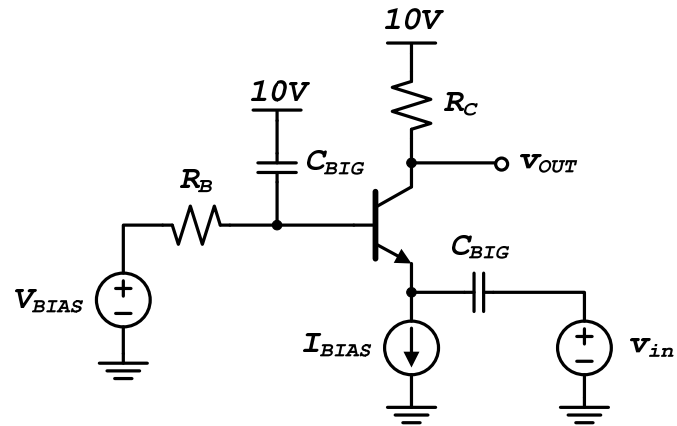
Initials: \_\_\_\_\_

- c) Assume the BJT is biased in the FAR region, and that  $I_{BIAS}$  is a DC bias source. Substitute the small-signal model for the BJT and find an expression for the small-signal gain  $a_v = v_{out}/v_{in}$ . Assume the BJT has finite  $V_A$  (include base-width modulation).



**Problem 2 (25 Points):** Use the circuit below and the values given in the table for all parts of this problem. The  $C_{BIG}$  capacitors should be treated as bypass capacitors.

$\beta_F = 100$
$V_A = \infty$
$V_{BE,ON} = 0.6V$
$V_{BIAS} = 5V$
$R_B = 10k\Omega$
$R_C = 1k\Omega$



- a) Draw the DC equivalent circuit. Calculate the value of  $I_{BIAS}$  that will bias the BJT in the FAR region, at the boundary between FAR and Saturation.

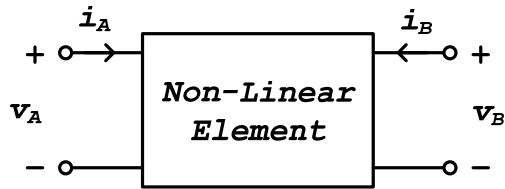
Initials: \_\_\_\_\_

- b) For this part only, assume the bias current  $I_C = 2.5mA$ . Draw the small-signal (ac) circuit and evaluate the values of the elements in the BJT small-signal model assuming “room temperature”. Assume  $V_A = \infty$ .

- c) For this part, do NOT use the evaluated values of small signal elements found in part b). Derive an expression for the midband small-signal gain  $a_v = v_{out}/v_{in}$ . Leave this expression in terms of variable names ( $r_\pi$ ,  $g_m$ , etc.). Assume  $V_A = \infty$ .



**Problem 3 (30 Points):** In this problem you will derive the small-signal (ac) model for a non-linear, 2-port element. For each part of this problem, use the device below with the given expressions for large-signal  $I$ - $V$  relationships. Show all your work.



for  $v_A > 0, i_A > 0, i_B > 0$

$$i_A = K v_A$$

$$v_B = \beta i_A^3 (1 + \rho i_B)$$

- a) Derive an expression to model the small-signal resistance at Port A,  $r_a = v_a / i_a$ , for the DC operating point:  $V_A, I_A, V_B$ , and  $I_B$ . Show all your work.

- b) Derive an expression to model the small-signal resistance at Port B,  $r_b = v_b/i_b$ , for the DC operating point:  $V_A$ ,  $I_A$ ,  $V_B$ , and  $I_B$ . Show all your work.

Initials: \_\_\_\_\_

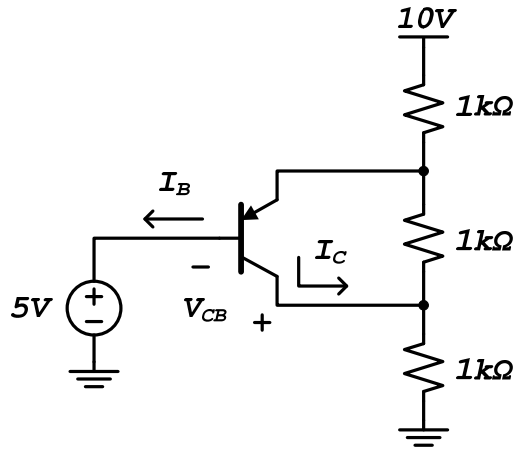
- c) Derive an expression to model the small-signal trans-resistance from Port A to Port B,  $r_m = v_b/i_a$ , for the DC operating point:  $V_A$ ,  $I_A$ ,  $V_B$ , and  $I_B$ . Show all your work.

d) Draw an equivalent circuit to model the small-signal response of the 2-port element.

**Problem 4 (25 Points):**

Use the circuit below and parameters given in the table for each part of this problem.

$\beta_F = 50$ $V_{EB,ON} = 0.6V$ $V_{EC,SAT} = 0.4V$ $V_A = \infty$
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- a) For this part, assume the BJT is in the Saturation region. Use the simplified model for the BJT in saturation, using the constant-voltage-drop model for the E-B junction and  $V_{EC,SAT}$ . Solve for the values of  $I_B$ ,  $I_C$ , and  $V_{CB}$  and enter them in the space below.

$I_B =$  \_\_\_\_\_

$I_C =$  \_\_\_\_\_

$V_{CB} =$  \_\_\_\_\_

- b) For this part, assume the BJT is in the FAR region. Use the simplified model for the BJT in FAR, using the constant-voltage-drop model for the E-B junction. Solve for the values of  $I_B$ ,  $I_C$ , and  $V_{CB}$  and enter them in the space below.

$$I_B = \underline{\hspace{2cm}}$$

$$I_C = \underline{\hspace{2cm}}$$

$$V_{CB} = \underline{\hspace{2cm}}$$

Initials: \_\_\_\_\_

- c) Based on your answers from parts a) and b), specify the correct region of operation of the BJT. Justify your answer.

(Space for additional work)