

Things to practice: working with random processes, mean functions, autocorrelation functions, stationarity, wide sense stationarity

Readings in random processes: Sections 6.1-6.5, except you may skip: multiple random processes on pp. 337,338, the Wiener process and Brownian motion on pp. 354-356, cyclostationary processes on pp. 363-366.

1. 6.14, p. 391
2. 6.15, p. 391
3. 6.16, a, p. 391,
4. 6.24, a,b p. 392 Notes: X_n 's are a Bernoulli random process. Skip the question: "Is the sample mean meaningful ...?"
5. 6.31, p. 393
6. 6.53, p. 395
7. 6.57, p. 396 (The "independence" of random processes $X(t)$ and $Y(t)$ means that every finite collection of X random variables are independent of every finite collection of Y random variables.)
8. Suppose $\{X_t\}$ is a wide sense stationary, continuous-time Gaussian random process with mean zero and autocorrelation function $R_X(\tau) = e^{-|\tau|}$.
 - (a) Find the probability that $|X(2) - X(5)| \leq 2$.
(Hint: Find the density of the random variable $Y = X(2) - X(5)$. Make good use of the fact that $X(2)$ and $X(5)$ are jointly Gaussian.)
 - (b) Find the covariance matrix for the random variables $X(t), X(t+1), X(t+2)$.

Other good problems: 6.17, 6.18, 6.19, 6.23, 6.25, 6.26, 6.32, 6.50, 6.51, 6.52, 6.55, 6.56, 6.58, 6.59, 6.66