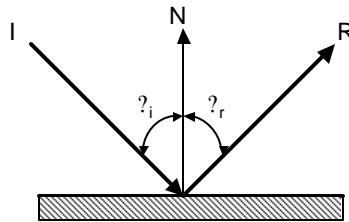




Ray Tracing II

Lecture
18

Ray Reflections



$$\vec{R} = \alpha \vec{I} + \beta \vec{N}$$

$$\theta_i = \theta_r$$

1



Ray Tracing II

Lecture
18

Ray Reflections

$$\vec{R} = \alpha \vec{I} + \beta \vec{N}$$

$$\theta_i = \theta_r$$

$$\cos(\theta_i) = \cos(\theta_r)$$

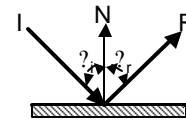
$$-\vec{I} \cdot \vec{N} = \vec{N} \cdot \vec{R}$$

$$-\vec{I} \cdot \vec{N} = \vec{N} \cdot (\alpha \vec{I} + \beta \vec{N})$$

$$-\vec{I} \cdot \vec{N} = \alpha \vec{N} \cdot \vec{I} + \beta \vec{N} \cdot \vec{N}$$

$$-\vec{I} \cdot \vec{N} = \alpha \vec{N} \cdot \vec{I} + \beta$$

$$-2(\vec{I} \cdot \vec{N}) = \beta$$



2



Ray Tracing II

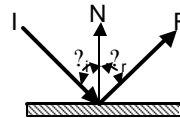
Lecture
18

Ray Reflections

$$-2(\vec{I} \cdot \vec{N}) = ?$$

$$\vec{R} = ?\vec{I} + ?\vec{N}$$

$$\vec{R} = \vec{I} - 2(\vec{N} \cdot \vec{I}) \vec{N}$$



3



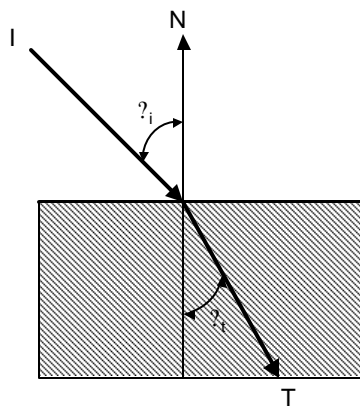
Ray Tracing II

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Ray Refraction

Snell's Law

$$\frac{\sin(\theta_i)}{\sin(\theta_t)} = \frac{n_2}{n_1}$$



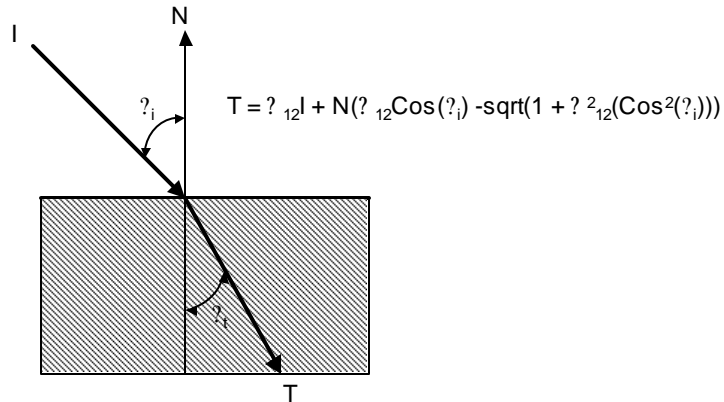
4



Ray Tracing II

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18

Ray Refraction



5



Ray Tracing II

Lecture
18

Shadows

To get shadows in ray tracing, at every intersection we shoot a test ray toward each light source.

If the ray gets to the light source then this light is used in the lighting calculation.

If the ray hits something then the light source is not used in the lighting calculation.

The ray direction used to test the light source can be used in the lighting calculation

6



Ray Tracing II

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18

Anti - Aliasing

- Sample More Rays
- Instead of Vectors use Truncated Cones, Rods, Pyramids
- Stochastic Sampling

7

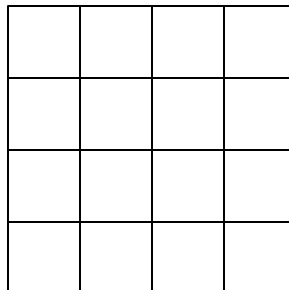


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Lecture
18

Anti - Aliasing

- Sample More Rays



8



Ray Tracing II

Lecture
18

Anti - Aliasing

- Instead of Vectors use Truncated Cones, Rods, Pyramids

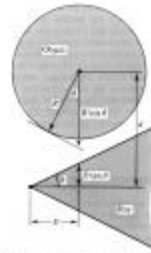


Figure 8.5 Ray-sphere intersection in ray tracing to ray is a cone.

If $D \cos \theta + \frac{R^2}{D} > 0$
where:
 D is the spread angle of the cone
 R is the radius of the sphere
 d is the distance between the point on the cone axis that is nearest to the center of the sphere
 D is the distance between this point on the cone axis and the cone origin

9

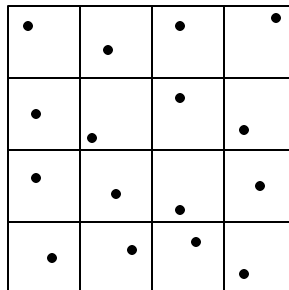


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18

Anti - Aliasing

- Stochastic Sampling



10



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Lecture
18

Anti - Aliasing

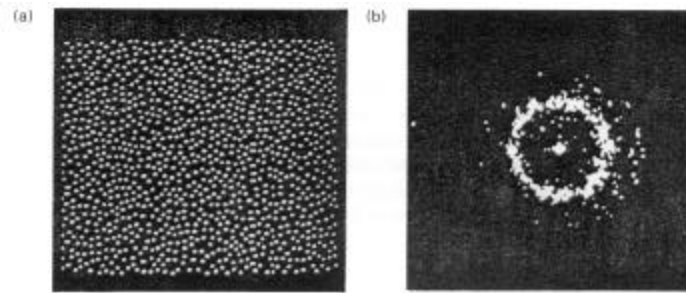


Fig. 3. (a) Monkey eye photoreceptor distribution. (b) Optical transform of monkey eye.

11



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Lecture
18

Temporal Anti - Aliasing

Motion Blur

Sub-pixel samples are stochastically sampled over time and space

12



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18

Temporal Anti - Aliasing



13



Ray Tracing II

Lecture
18

Temporal Anti - Aliasing



14



Ray Tracing II

Lecture
18

Forward Ray Tracing

This means tracing rays from the light source into the scene.

- This can be very expensive
- But adds effect that can only be found if this is done.
- One of the ways to get water caustics

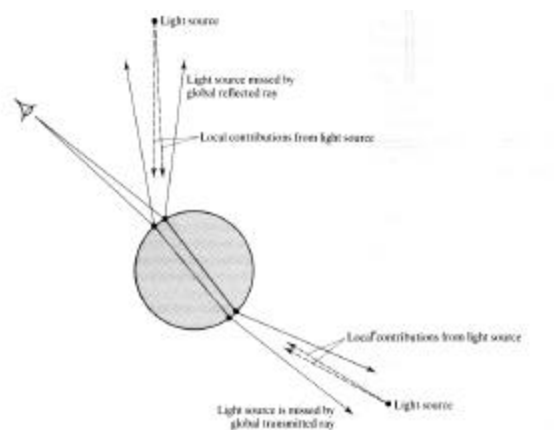
15



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Lecture
18

Forward Ray Tracing



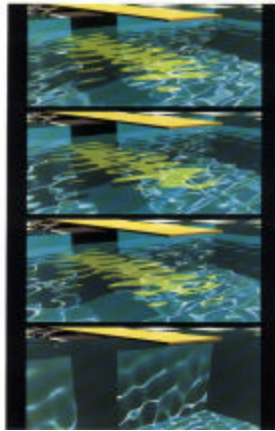
16



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Lecture
18

Forward Ray Tracing



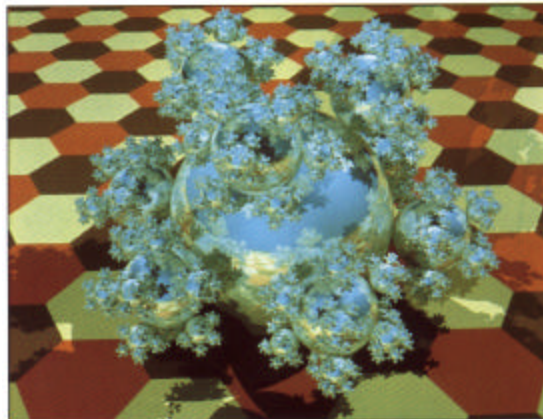
17



Ray Tracing II

Lecture
18

Sphereflake



18



Ray Tracing II

Lecture
18

MinRay

```
typedef struct{double x,y,z;}vec;vec U,black,amb={.02,.02,.02};struct sphere{
vec cen,color;double rad,kd,ks,kt,kl,ir}*s,*best,sph[]={0,.6,.5,1,1,1,.9,
.05,.2,.85,0,.1,7,-1,.8,-.5,1,.5,.2,1,.7,.3,0,.05,1,2,1,.8,-.5,1,.8,.8,
1,.3,.7,0,.0,.1,2,3,-.6,.15,.1,.8,1,.7,.0,.0,.0,.6,1.5,-3,-3,.12,.8,1,
1,.5,.0,.0,.0,.5,1.5,};yx;double u,b,tmin,sqrt(),tan();double vdot(A,B)vec A
,B;{return A.x*B.x+A.y*B.y+A.z*B.z;}vec vcomb(a,A,B)double a;vec A,B;{B.x+=a*
A.x;B.y+=a*A.y;B.z+=a*A.z;return B;}vec vunit(A)vec A;{return vcomb(1./sqrt(
vdot(A,A)),A,black);}struct sphere*intersect(P,D)vec P,D;{best=0;tmin=1e30;s=
sph+5;while(s-->sph)b=vdot(D,U=vcomb(-1.,P,s->cen)),u=b*b-vdot(U,U)+s->rad*s
->rad,u=u>0?sqrt(u):1e31,u=b-u>1e-7?b-u:b+u,tmin=u>1e-7&&u<tmin?best=s,u:
tmin;return best;}vec trace(level,P,D)vec P,D;{double d,eta,e;vec N,color;
struct sphere*s,*l;if(!level--)return black;if(s=intersect(P,D))else return
amb;color=amb;eta=s->ir;d=-vdot(D,N=vunit(vcomb(-1.,P=vcomb(tmin,D,P),s->cen
)));if(d<0)N=vcomb(-1.,N,black),eta=1/eta,d=-d;l=sph+5;while(1-->sph){if((e=1
->kl*vdot(N,U=vunit(vcomb(-1.,P,l->cen))))>0&&intersect(P,U)=1)color=vcomb(e
,l->color,color);U=s->color;color.x*=U.x/color.y*=U.y/color.z*=U.z/e=1-eta*
eta*(1-d*d);return vcomb(s->kt,e>0?trace(level,P,vcomb(eta,D,vcomb(eta*d-sqrt
(e),N,black)):black,vcomb(s->ks,trace(level,P,vcomb(2*d,N,D)),vcomb(s->kd,
color,vcomb(s->kl,U,black)))));}main(){printf("%d %d\n",32,32);while(yx<32*32)
U.x=yx*32-32/2,U.z=32/2-yx++/32,U.y=32/2/tan(25/114.5915590261),U=vcomb(255.,
trace(3,black,vunit(U)),black),printf("%.0f %.0f %.0f\n",U);/*minray!*/}
```

19



Ray Tracing II

Lecture
18

MinRay

Those who entered the contest also learned some repetitive C coding tricks:

- `color = point; struct {float r, g, b;} => struct {float x, y, z;}`
- pass structures (not just pointers to structs) to allow vector expressions
- use global variables for return values
- no optimizations: trace specular and transmitted rays even if `coefficient=0!`
- reuse variables!
- for: `{i=0; i<n; i++} => i = n; while (i--)`
- merge x and y loops into one
- nonzero statics are initialized to 0
- `sph[i] => sph+i`
- choose just the right set of utility routines
- creative use of constants, e.g.: `if (a) {b;c;} => if (a) b,c;`
- move assignments into expressions: `b = vdot(D, U = vcomb(-1., P, s->cen))`

(Creative (non-portable) C):

- eliminate redundancies in `struct del struct {int a;} => struct {int a}`
- nonzero right-to-left argument evaluation order

Winner of the most shocking cheat award, a little gem by Joe Cyckow:

- `printf("If %f %f", pt.x, pt.y, pt.z); => printf("If %f %f", pt.x, pt.z);`

Since Joe Cyckow said this was only his second C program (!), I asked him how he managed to do so well. He responded:

"My primary program language is FORTRAN and COMPAQ (CDC assembly) for the CYBER 320 and the CYBER 800s... This is an interesting way to learn C. I spent the weekend looking through Kernighan & Ritchie trying to determine if what I wanted to do was legal C. Finally, Kirk took time to show while we were sitting in a bar."

But if you were expecting a useful ray tracing program out of this, a warning: as one would expect of any "minimal" program, the winning program is cryptic, inefficient, unmaintainable, and nearly useless except as a source of C coding tricks. If you want a good ray tracer, look elsewhere!

20

