

1.1 Deduce the following expressions for  $k_F$ ,  $n(E_F)$  and  $D(E_F)$  for 1, 2, and 3 dimensional systems.

Dimension	$k_F$	$n(E_F)$	$D(E_F)$
3	$(3\pi^2 n)^{1/3}$	$\frac{1}{3\pi^2} \left( \frac{2mE_F}{\hbar^2} \right)^{3/2}$	$\frac{1}{2\pi^2} \left( \frac{2m}{\hbar^2} \right)^{3/2} \sqrt{E_F}$
2	$\sqrt{2\pi n}$	$\frac{m}{\pi\hbar^2} E_F$	$\frac{m}{\pi\hbar^2}$
1	$\frac{\pi n}{2}$	$\frac{2}{\pi\hbar} \sqrt{2mE_F}$	$\frac{\sqrt{2m}}{\pi\hbar} \frac{1}{\sqrt{E_F}}$

1.2 Calculate the Fermi wavelength (De Broglie wavelength at the Fermi surface) for two conductors with carrier density of  $10^{23} \text{ cm}^{-3}$  (a metal) and  $10^{18} \text{ cm}^{-3}$  (a semiconductor), respectively. Which of the two systems will be first to exhibit quantum size effects as the sample sizes are reduced?

1.3 Calculate the scattering time and the mean free path of Cu at room temperature, which has a carrier density  $n = 8.47 \times 10^{22} \text{ cm}^{-3}$ , and resistivity  $\rho = 1/\sigma = 1.72 \mu\text{m}\cdot\text{cm}$ .