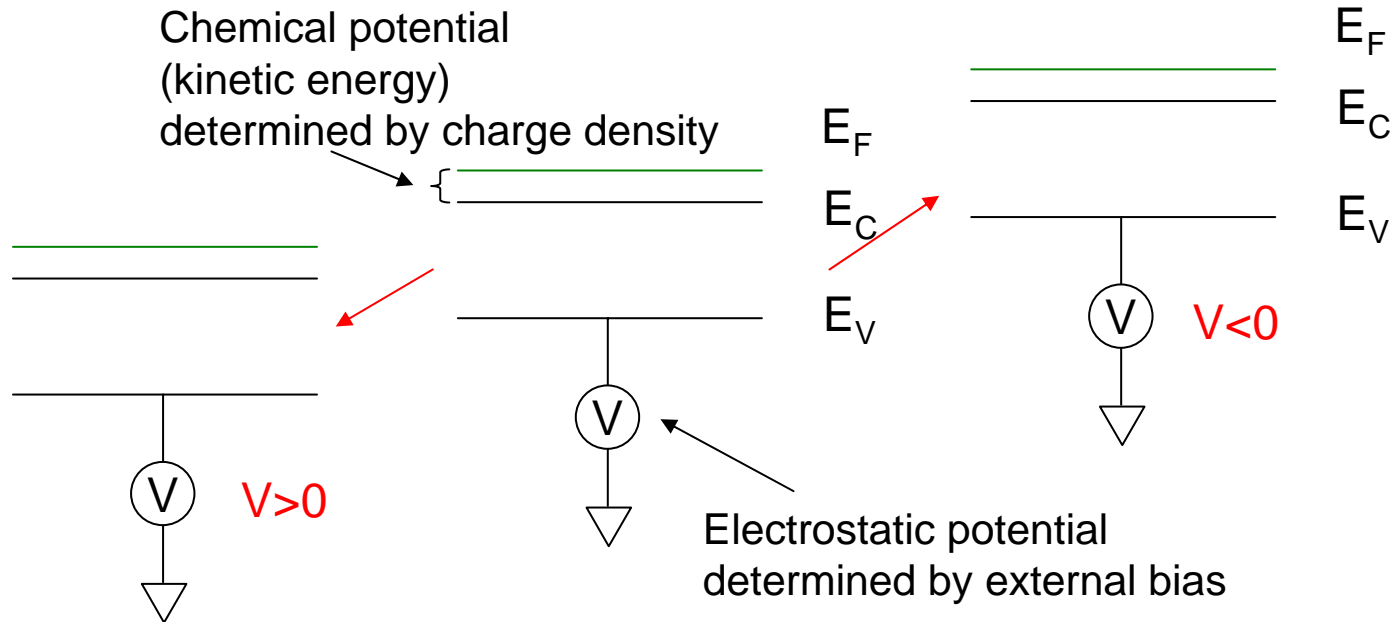


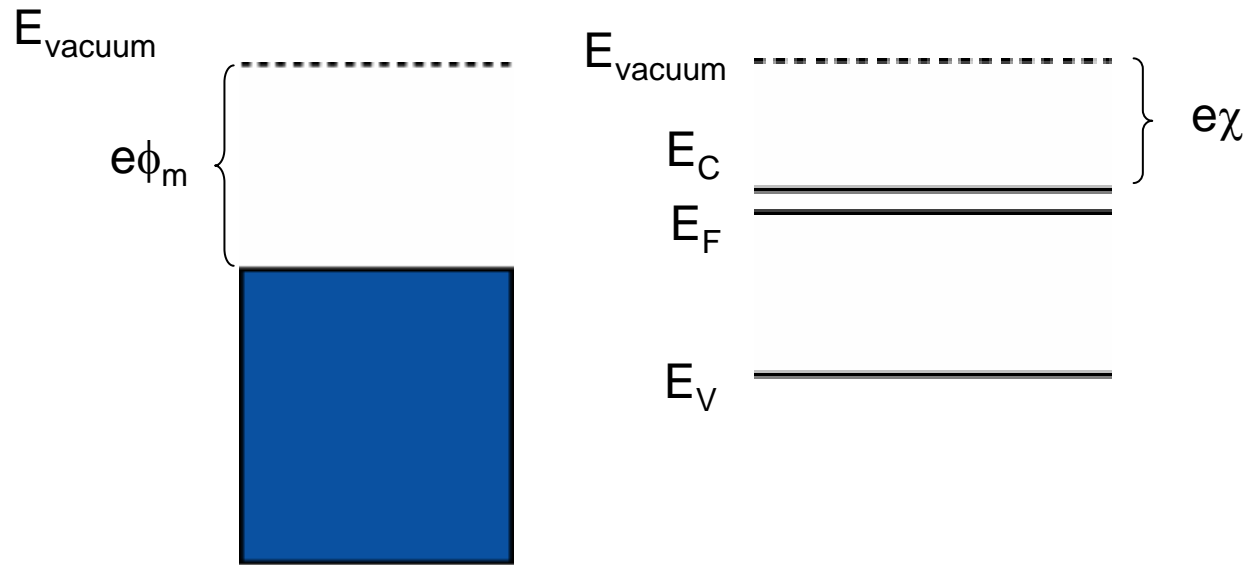
## A few words about drawing the energy levels



$E_F$ , electrochemical potential  
 = chemical potential + electrostatic potential (bias) + constant

Energy levels are referred to electrons!  $\Phi = (-e) \cdot V$   
 positive bias, levels  $\downarrow$       negative bias, levels  $\uparrow$

## About the constants



Work function  $e\phi_m$ : the amount of energy required to take an electron from the Fermi level within a material and remove it to infinity. Concept more useful for metals.

Electron affinity  $e\phi_m$ : the energy difference between the bottom of the conduction band and the vacuum level. Concept more useful for semiconductors since  $E_F$  depends on carrier density.

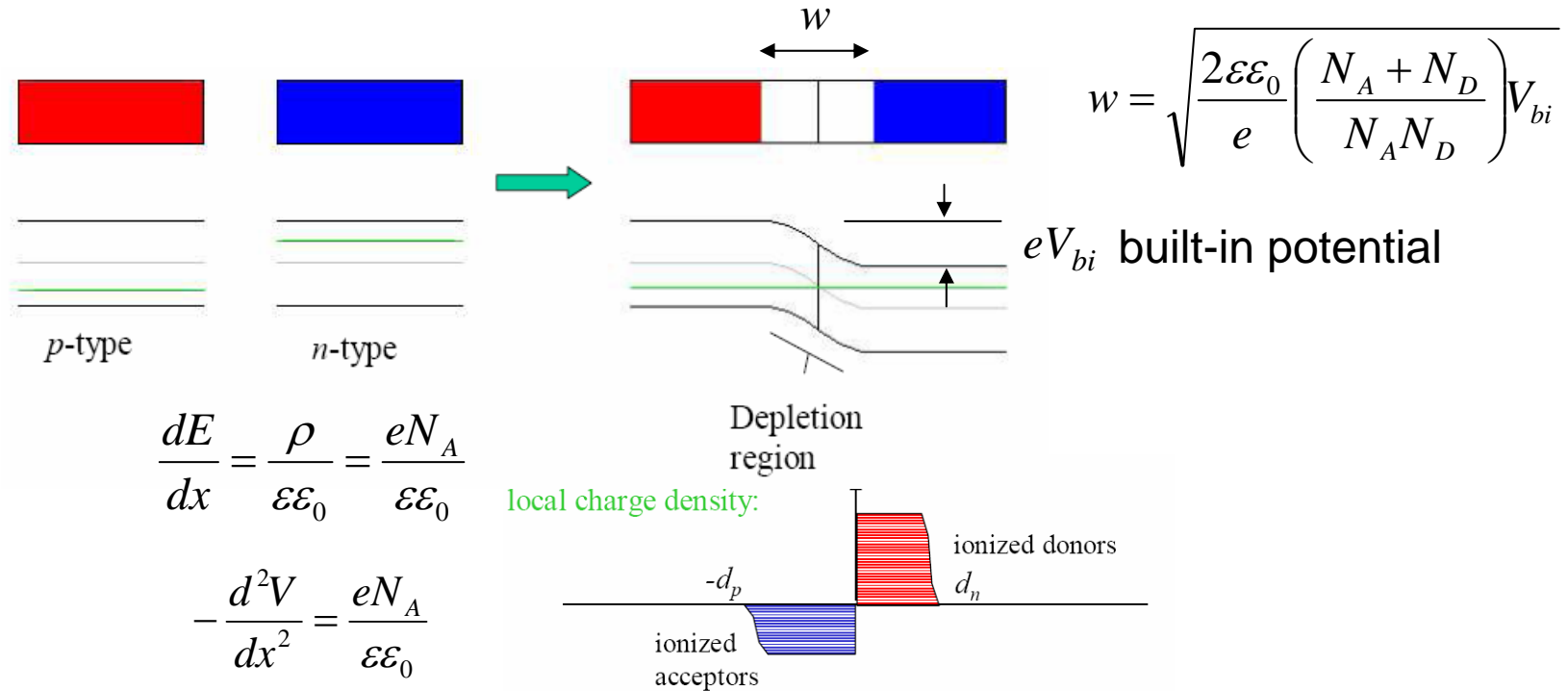
## Joining materials with different Fermi levels

- Electrochemical potential needs to line-up
- Can get appreciable charge transfer, causing local changes in band structure!
- Many energy scales to contend with:  $E_F$ ,  $E_C$ ,  $E_V$ ,  $\Phi$  on both sides of junction, etc.
- Certain common situations arise in technology....

<http://home3.netcarrier.com/%7Echan/SOLIDSTATE/BANDS/bands.html>

# Semiconductor-semiconductor junctions

One of the most commonly used: the  $p$ - $n$  junction



Many possibilities exist. Play with the java program below.

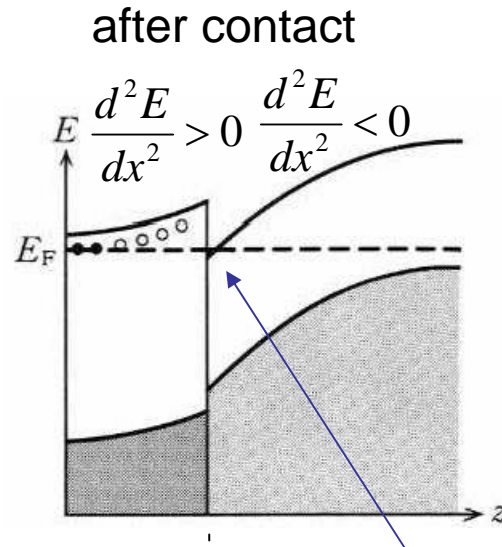
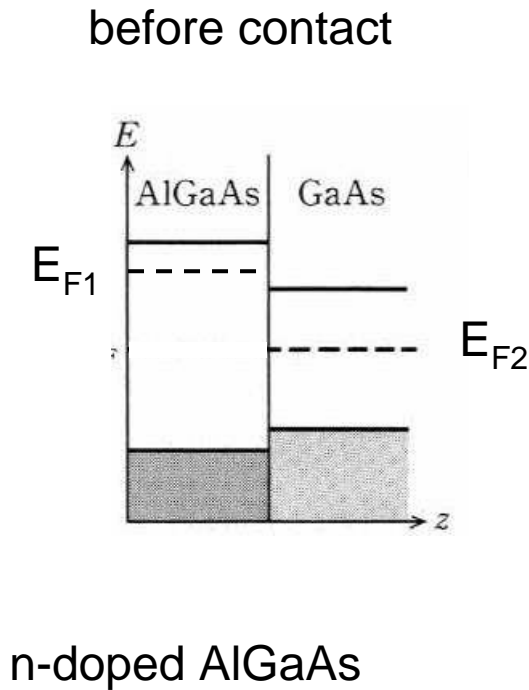
<http://home3.netcarrier.com/%7Echan/SOLIDSTATE/BANDS/bands.html>

# Semiconductor-semiconductor junctions

## GaAs/AlGaAs heterostructure interface

$$\frac{d^2 E}{dx^2} = \frac{eQ}{\epsilon\epsilon_0}$$

$E$ , electron energy  
 $Q$ , net charge



$$\frac{d^2 E}{dx^2} < 0 (> 0)$$

for net negative  
 (positive) charge  
 determines band  
 shape

two-dimensional electron gas  
 (2DEG)

↔ confined in Z direction

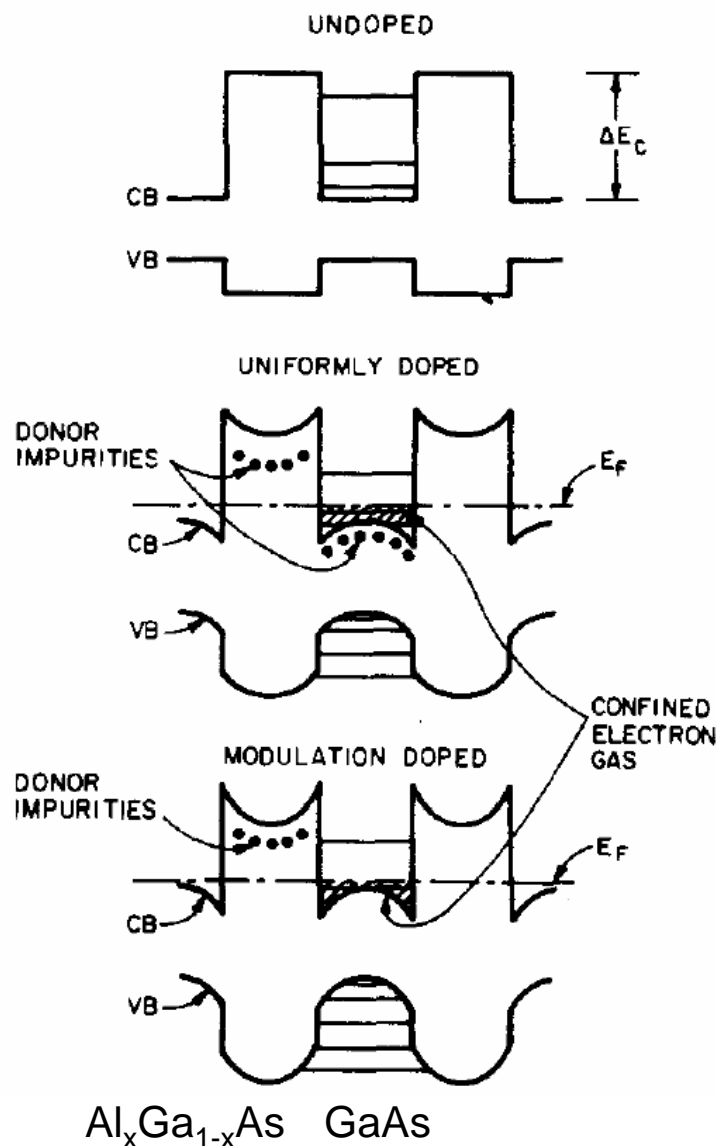
↑↓ free in X,Y direction

## Modulation doping

Undoped  $\text{Al}_x\text{Ga}_{1-x}\text{As}$  layer as spacer layer to further minimize dopant scattering. ( $\delta$  doping)

World record  $\mu = 1.4 \times 10^7 \text{ cm}^2/\text{Vs}$ ,  
mean free path  $120 \mu\text{m}$ .  
Umansky, APL, 71, 683 (1997)

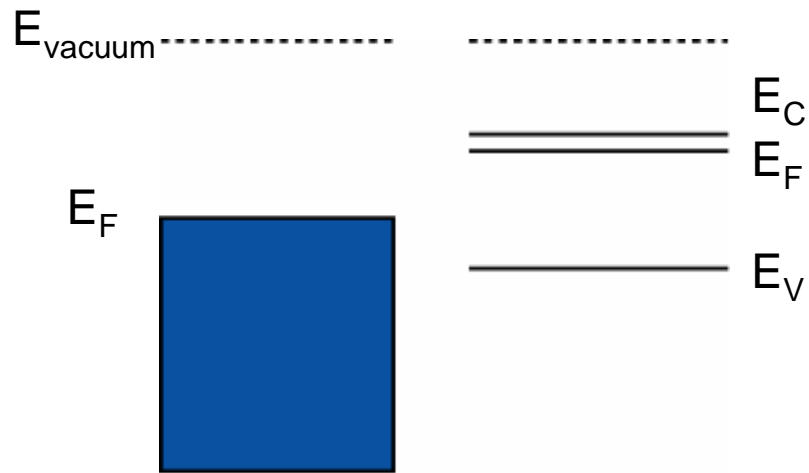
Si:  $\mu \sim 1500 \text{ cm}^2/\text{Vs}$



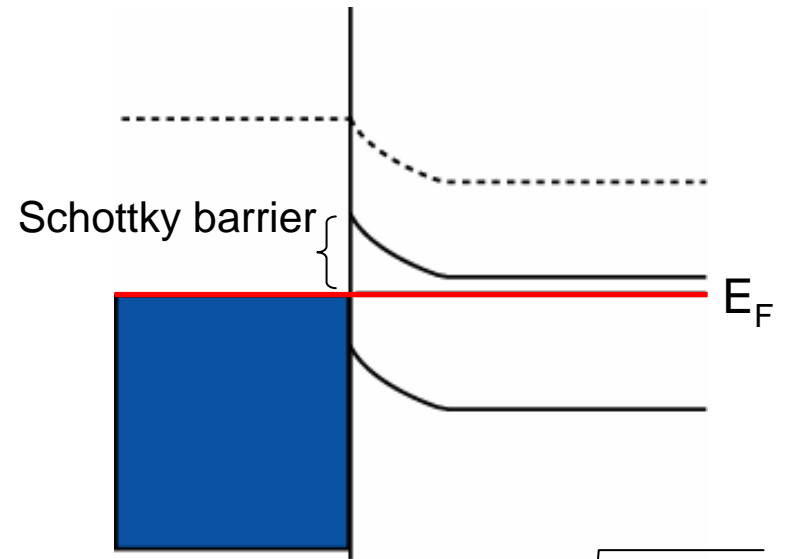
Dingle, APL, 33, 665 (1978)

# Metal-semiconductor junctions

before contact



after contact



$$w = \sqrt{\frac{2\epsilon\epsilon_0 V_{bi}}{eN_D}}$$

$$\text{Schottky barrier height} = e\phi_m - e\chi$$

## Surface and interface states summary

- Surface states and interface states exist when symmetry of infinite periodic lattice is broken.
- Normally located inside the band gap, and close to mid gap

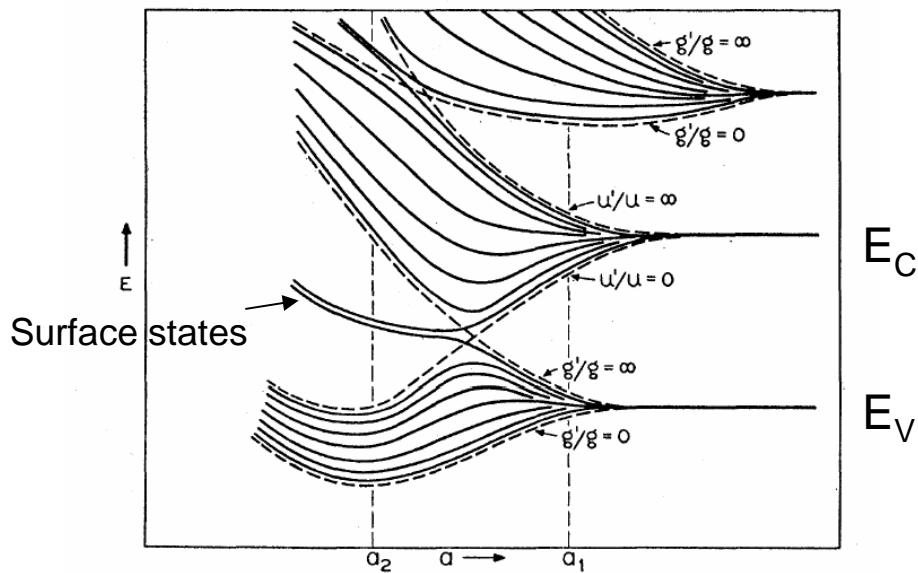
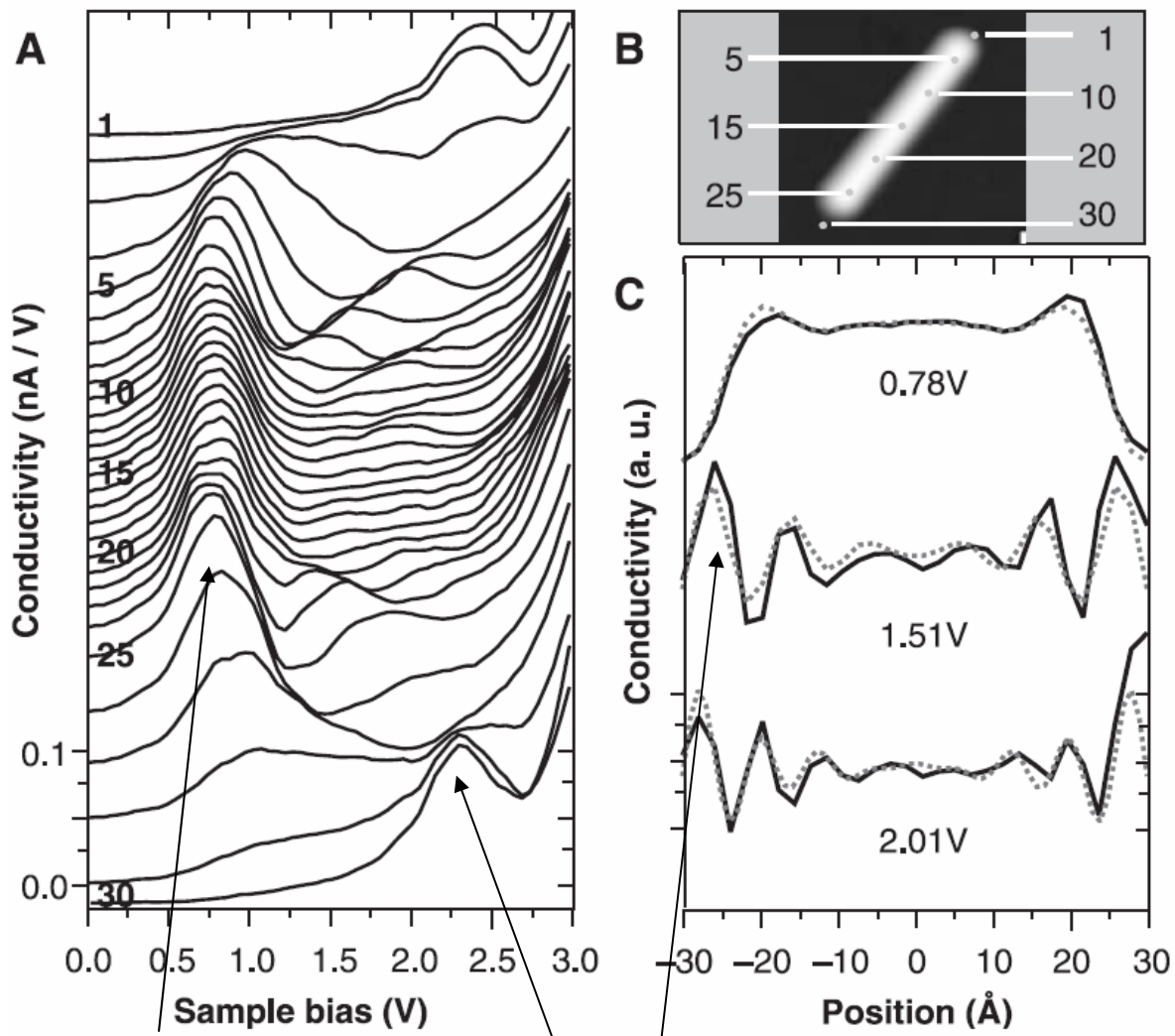


FIG. 2. Energy spectrum for a one-dimensional lattice with eight atoms.



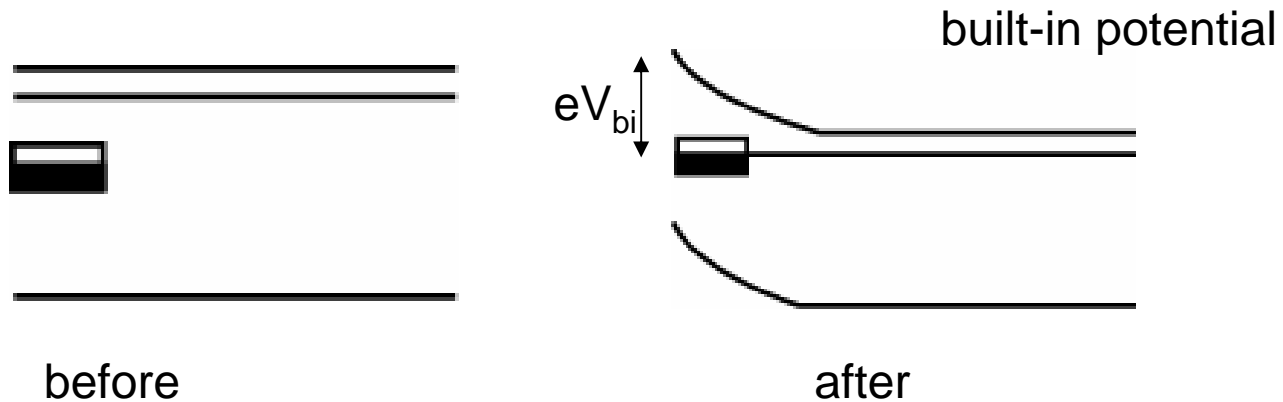


$E_V$

defect states (like surface states)

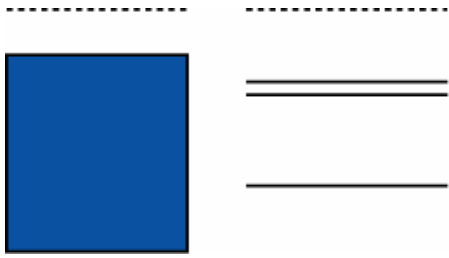
## Surface and interface states summary

- Density of surface states can be very high: number of surface states can be comparable to number of atoms on surface!
- Surface states normally partially filled. Charges need to flow from bulk in to empty surface states until Fermi level line-up (Fermi level pinning)

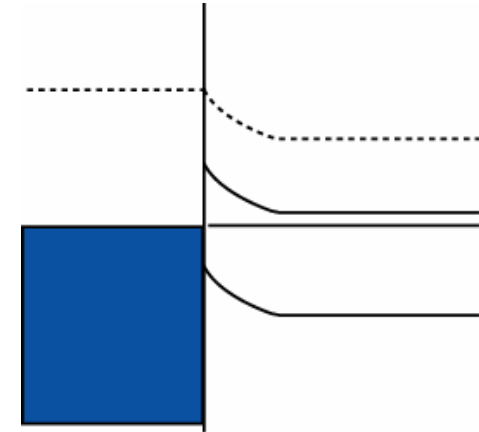
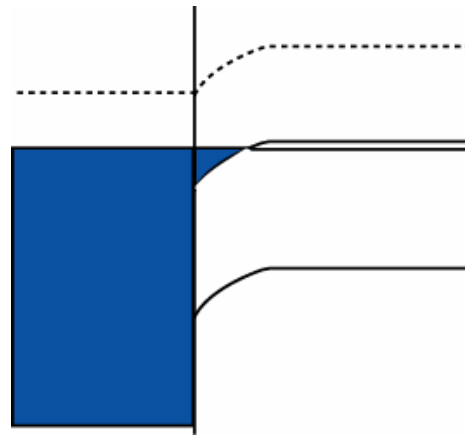


# Ohmic contacts

before



after



True Ohmic contacts, hard to obtain due to interface states (which always pins the Fermi level close to mid gap).

Effective Ohmic contacts, electrons can directly tunnel through the depletion region

$$w = \sqrt{\frac{2\epsilon\epsilon_0 V_{bi}}{eN_D}}$$