

**ASSIGNED:** Mar. 31, 2006. **READ:** Part 8 of Official Lecture Notes (available on-line).  
**DUE DATE:** Apr. 07, 2006. **TOPICS:** Poles & zeros & frequency response; exam review.

Show work on separate sheets of paper. Include all hand and Matlab plots and code.  
 This entire problem set consists of problems from previous EECS 206 Exams #3.

- [10] 1. Rewrite  $\frac{1}{2}(1+j)(j)^n + \frac{1}{2}(1-j)(-j)^n$  entirely in terms of sinusoids.
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- [10] 2. Determine a (2,2) ARMA difference equation having the gain function  
 $|H(e^{j\omega})| = \sqrt{(3+4\cos\omega)^2 + 16\sin^2\omega} / \sqrt{(1+2\cos\omega)^2 + 4\sin^2\omega}$ .
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- [10] 3. Determine the simplest MA system that eliminates  $3\cos(\frac{\pi}{2}n) + 4\cos(\pi n)$ .
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- [10] 4. A system has difference eqn.  $5y[n] + 3y[n-1] + y[n-2] = 7x[n] + 6x[n-1] - x[n-2]$ .  
 Compute the response  $y[n]$  if the input  $x[n] = 9 + 2\cos(\frac{\pi}{2}n) + 3\cos(\pi n)$ .
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- [10] 5. System has pole      Output  $y[n] = 9\delta[n-1]$   
 -zero diagram :      if the input  $x[n] =$  what?       $\underbrace{X}_{-2/3} - \underbrace{X}_{-1/3} \text{ --- } \underbrace{O}_1$
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- [10] 6. Compute the inverse z-transform of  $\frac{z^2-5z+6}{z^2(z-1)}$ . **Hint:** Do not use partial fractions.
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- [10] 7. The filter eliminating  $\omega = \frac{\pi}{3}$  and  $\omega = \frac{2\pi}{3}$  has impulse response  $h[n] = ?$
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- [10] 8. Draw the **pole-zero plot** for a filter that will eliminate a signal having period=8 while having as little effect as possible on any other signals that may be present.
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- [10] 9.  $[(z-0.7)(z^2+1)(z+1)] / [(z-0.8e^{j\pi/3})(z-0.8e^{-j\pi/3})(z-0.9e^{j3\pi/4})(z-0.9e^{-j3\pi/4})]$ .  
 Sketch the relative magnitude of its frequency response (i.e., gain function).
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- [10] 10.  $x[n] \rightarrow \overline{y[n] = x[n] + x[n-1] + x[n-2] + \dots + x[n-5] + x[n-6] + x[n-7]} \rightarrow y[n]$   
 Here input  $x[n]$  is a zero-mean, real-valued, and periodic signal having period=8.  
 Make a stem plot of  $y[n]$ . Don't worry about the vertical scale.

“Demographer: someone who thinks the average Miamian is born Cuban and dies Jewish.”