NOTE: All angles are in degrees. All impedances are in Ohms. All frequencies are in $\frac{rad}{sec}$

1a.
$$Z = 12 + j50(0.1) = 12 + j5$$
. $I = \frac{V}{Z} = \frac{26\angle 0}{13\angle 22.6} = 2\angle -22.6$. $i(t) = 2\cos(50t - 22.6)$.
1b. $\frac{1}{2}|I|^2Re[Z] = \frac{1}{2}2^2(12) = 24$. OR: $\frac{1}{2}Re[VI^*] = \frac{1}{2}Re[26(2\angle -22.6)] = 26\cos(22.6) = 24$.
1c. $Y = \frac{1}{Z} = \frac{1}{12+j5} = \frac{12-j5}{13^2}$. NEED: $-j5/13^2 + j50C = 0 \rightarrow C = 5/[(50)(13^2)] = 592\mu F$.

1b.
$$\frac{1}{2}|I|^2Re[Z] = \frac{1}{2}2^2(12) = 24$$
. OR: $\frac{1}{2}Re[VI^*] = \frac{1}{2}Re[26(2\angle -22.6)] = 26\cos(22.6) = 24$.

1c.
$$Y = \frac{1}{Z} = \frac{1}{12+i5} = \frac{12-j5}{13^2}$$
. NEED: $-j5/13^2 + j50C = 0 \rightarrow C = 5/[(50)(13^2)] = 592\mu F$.

2a.
$$V_{OC} = \frac{3/(j\omega C)}{j\omega L + \frac{1}{j\omega C}} = \frac{3}{1 - \omega^2 LC}$$
. $Z = (j\omega L)||\frac{1}{j\omega C} = \frac{L/C}{j\omega L + \frac{1}{j\omega C}} = \frac{j\omega L}{1 - \omega^2 LC}$. $I_{SC} = \frac{3}{j\omega L}$.

2b.
$$\omega = 0 \to (L \to \text{short}, C \to \text{open})$$
 or plug in (a). Pure voltage source.

2c.
$$\omega = \frac{1}{\sqrt{LC}} \rightarrow 1 - \omega^2 LC = 0 \rightarrow (V_{OC} \& Z \rightarrow \infty)$$
. Pure current source.

3a.
$$V_O(t) = 6\frac{3}{0+3} + 9\sqrt{2}\frac{3}{|3+j3|}\cos(3t - \tan^{-1}(\frac{3}{3})) + 20\frac{3}{|3+j4|}\cos(4t - \tan^{-1}(\frac{4}{3})).$$

3a. Simplifies to
$$V_O(t) = 6 + 9\cos(3t - 45^\circ) + 12\cos(4t - 53^\circ)$$
.

3b. RC lowpass filter
$$\to H(j\omega) = \frac{1/(j\omega C)}{R + \frac{1}{j\omega C}} = \frac{1/(RC)}{j\omega + \frac{1}{RC}}.$$
 $\frac{1}{RC} = 3 \to C = \frac{1}{3}F.$

3c. DC:
$$\frac{1}{3} = \frac{A}{0+B}$$
. $B = 6 \to A = 2, C = \frac{\sqrt{2}}{6}$. $A = 2, B = 6, C = \frac{\sqrt{2}}{6}$.

4ab.
$$Q = \frac{100}{103-97} = 16.7$$
. $\omega_o = 2\pi 10^6$. $Q = \frac{\omega_o L}{R} = \frac{2\pi 10^6 L}{20} = 16.7 \rightarrow L = \frac{(16.7)(20)}{2\pi 10^6} = 53\mu H$.
4c. $\omega_o = \frac{1}{\sqrt{LC}} \rightarrow C = \frac{1}{L\omega_o^2} = 1/[(53 \cdot 10^{-6})(2\pi 10^6)^2] = 478pF$.

4d.
$$\mathbf{f} \to \mathbf{0} : |H(j2\pi f)| \simeq 2\pi fRC = 2\pi (20\Omega) 478pF = 6 \times 10^{-8} f \to f_1 = \frac{1}{60} MHz$$

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$$\mathbf{f} \to \mathbf{0} : |H(j2\pi f)| \simeq 2\pi fRC = 2\pi (20\Omega) 478 pF = 6 \times 10^{-8} f \to f_1 = \frac{1}{60} MHz$$

4d. $\mathbf{f} \to \infty : |H(2\pi f)| \simeq \frac{R}{2\pi fL} = \frac{20\Omega}{53\mu H(2\pi f)} = \frac{6\times 10^4}{f} \to f_2 = 60 MHz. \quad 1 MHz = \sqrt{f_1 f_2}.$

5a. **Zeros:** 0.3. **Poles:** 3;300.
$$H(j\omega) = C \frac{j\omega + 0.3}{(j\omega + 3)(j\omega + 300)}$$
. $1 = C \frac{0.3}{3(300)} \to C = 3000$.

5a. **Zeros:** 0.3. **Poles:** 3;300.
$$H(j\omega) = C \frac{j\omega + 0.3}{(j\omega + 3)(j\omega + 300)}$$
. $1 = C \frac{0.3}{3(300)} \to C = 3000$.
5b. $H(j\omega) = -\frac{Z_F}{Z_I} = -\frac{3000 + \frac{1}{j\omega \frac{1}{900}}}{303 + j\omega(1) + \frac{1}{j\omega \frac{1}{900}}} = -\frac{3000(j\omega + 0.3)}{(j\omega)^2 + 303(j\omega) + 900}$. $H(j\omega) = \frac{3000(j\omega + 0.3)}{(j\omega + 3)(j\omega + 300)}$.

NOTE: Answers to #5a and #5b agree (to a sign, which could easily be present).

SCORES: 96[2],95[5],93,91[5],90[2],89[3],88,87,86[4],84,83,82,80[3],79,78[2],

SCORES: 77[2],75[2],73,71,70,68,64[2],63,61,60,58,55,51,45,40,38,34,30.

MEDIAN: 80. GRADING COMMENTS BELOW. Have a good summer!

- 1. A few used Z = 12 + j0.1 (forgot $\omega = 50$); this was -2. Most got it (you better!).
- 1. A few used impedance instead of admittance in #1c; got bogged down in algebra.
- 2. Some wrote $V_{OC} = \frac{3\cos(\omega t)}{1-\omega^2 LC}$ and $Z = \frac{j\omega L}{1-\omega^2 LC}$. Never mix time and phasor domains! I didn't take off points for this (I probably should have). Few got #2c (oh well).
- 3. Most got these, of course, but almost 20% couldn't get it (that's pretty bad).
- 4. Several omitted $2\pi \to L = 333\mu H$, C = 3nF; 7/10 for this. Only 5 got #4c (oh well).
- 5. A few thought there was a pole or zero at $\omega = 30,000$ (certainly not on the plot).