

1. Radio: $12.5 = V_T(\frac{6.25}{R_T+6.25})$. Headlights: $11.7 = V_T(\frac{0.65}{R_T+0.65})$.

Solving 2 equations in 2 unknowns $\rightarrow V_T = 12.6V$ and $R_T = 0.05\Omega = 50m\Omega$.

2a. Node equation at a: $1.5 = \frac{V_a}{60+20} + \frac{V_a-30}{40} \rightarrow V_a = 60V \rightarrow V_{OC} = V_a \frac{60}{60+20} = 45V$.

2a. Node equation at a: $1.5 = \frac{V_a}{20} + \frac{V_a-30}{40} \rightarrow V_a = 30V \rightarrow I_{SC} = \frac{V_a}{20} = 1.5A$.

2b. Setting $30V \rightarrow$ short and $1.5A \rightarrow$ open $\rightarrow R_T = 60 \parallel (40 + 20) = 30\Omega$.

This is consistent with the results of (a): $R_T = \frac{V_{OC}}{I_{SC}} = \frac{45V}{1.5A} = 30\Omega$.

3. $8mA \parallel 20k\Omega \parallel 30V = 30V$. Thevenin $\{30V, 15k\Omega\} \rightarrow$ Norton $\{2mA, 15k\Omega\}$.

Combining current sources and resistors \rightarrow Norton $\{-8mA, 30 \parallel 15 = 10k\Omega\}$.

4. Since no independent sources, Thevenin equivalent has $V_T = 0$ (pure resistor).

Connect up 1V source: Node eqn. $\rightarrow \frac{V-1}{20} + \frac{V}{80} + \frac{V-40(-V/80)}{16} = 0 \rightarrow V = 0.32V$.

$I = \frac{1-0.32}{20} + \frac{1-40i\Delta}{60} = 0.034A + \frac{1-40(-0.32/80)}{60} = 0.0533A \rightarrow R_T = \frac{1V}{0.0533A} = 18.75\Omega$.

5a. This is what "maximum power transfer" *isn't*. $R_o = 0$ maximizes $P_{6\Omega} = i^2(6\Omega)$.

5b. This is what it *is*. Now we vary the load, not the source, resistance. $R_o = 6\Omega$.

6. Thevenin equivalent resistance=Norton equivalent resistance= $10k\Omega$, so load= $10k\Omega$.

7a. $V_T = 30(\frac{8 \parallel 8+8}{2+(8 \parallel 8+8)}) = \frac{180}{7}V$. $I_{SC} = \frac{30V}{2\Omega} = 15A$. $R_T = 2 \parallel (8 \parallel 8 + 8) = 2 \parallel 12 = \frac{12}{7}\Omega$.

7b. KVL: $\frac{180}{7} - \frac{12}{7}I - \frac{96}{I} = 0 \rightarrow I^2 - 15I + 56 = 0 \rightarrow I = 7A, 8A \rightarrow V = \frac{96}{7}V, 12V$

Note there are *two* possible solutions, since the i-v characteristic is nonlinear.