## **APPLICATION OF WAVELETS AND FRACTALS** TO DETECTION OF CARDIAC ANOMALIES

**PROBLEM:** Detection of irregular heartbeat (premature ventricular contraction (PVC)).

- 1. Can lead to arrhythmia and heart attacks.
- 2. PVC localized in time, yet its high frequencies are indistinguishable from normal heartbeats. How to find?

**SOLUTION:** Take Daubechies wavelet transform.

- 1. Fine scales can't distinguish PVC from normal.
- 2. Coarse scales CAN detect PVC from normal heartbeats.

**PROBLEM:** Stenosis (narrowing of arteries) from too much cholesterol, etc. $\rightarrow$ blockage.

**IDEA:** Stenosis $\rightarrow$ turbulence $\rightarrow$ heartSOUNDS.

- 1. Turbulence tends to be *fractal*:  $\sigma_{x(at)}^2 = a^{-2H} \sigma_{x(t)}^2$ where H=Hurst exponent; (2 - H)=fractal dimension.
- 2. Wavelet xform  $x_n^m = \int x(t) 2^{m/2} \psi(2^m t n) dt$ . a. x(t) fractal $\rightarrow \sigma_{x_n^m}^2 = 2^{-(2H+1)m} \sigma^2$ . b. Log-log plot of  $\sigma_{x_m}^2$  vs. scale  $m \to H$  from slope. **SOLUTION:** Compute variance in n of  $x_n^m$ .
- 1. Assume detail signals  $x_n^m$  are stationary in n. 2. PVC $\rightarrow$ fractal $\rightarrow \sigma_{x_n^m}^2 = 2^{-(2H+1)m}\sigma^2$ .
- 3. (2 H)=fractal dimension= $\begin{cases} 1.45 & \text{for normal} \\ 1.95 & \text{for PVC} \end{cases}$ Also, PVC $\rightarrow$ line on log-log plot; normal $\rightarrow$ no line

See over for plots; IEEE Spectrum May 1997 for details.