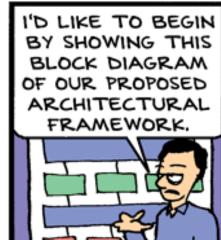
In Our Last Exciting Episode

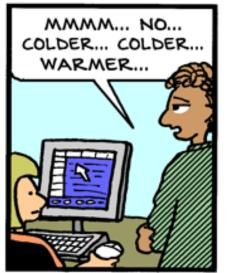












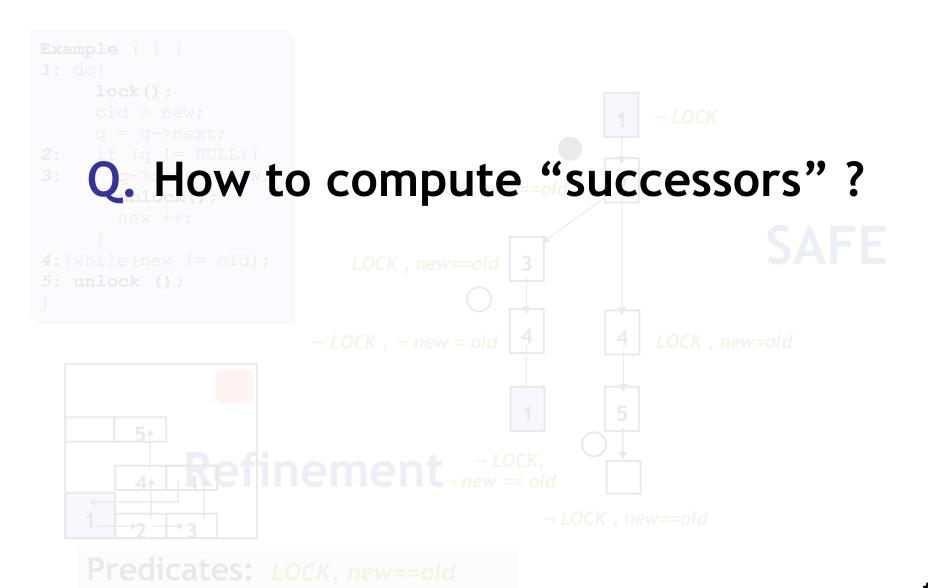




Bug Bash by Hans Bjordahl http://www.bugbash.net/

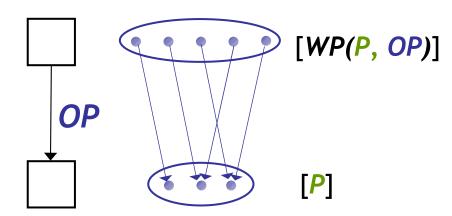
#1

Two SLAM/BLAST handwaves



Weakest Preconditions

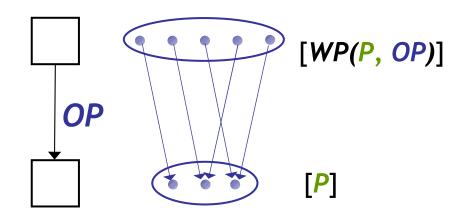
```
WP(P,OP)
Weakest formula P' s.t.
if P' is true before OP
then P is true after OP
```

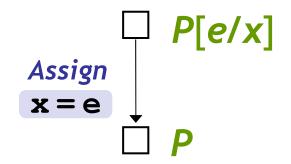


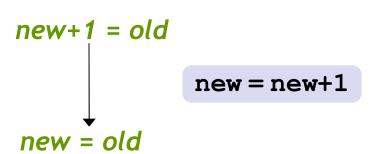
Weakest Preconditions

WP(P, OP)

Weakest formula *P'* s.t. if *P'* is true <u>before</u> *OP* then *P* is true <u>after</u> *OP*







How to compute successor?

```
Example ( ) {
    1: do{
        lock();
        old = new;
        q = q->next;

2: if (q != NULL) {
    3:        q->data = new;
        unlock();
        new ++;
    }

4:}while(new != old);

5: unlock ();
}
```

```
LOCK, new==old \boxed{3} F

OP

- LOCK, ¬ new = old \boxed{4} ?
```

For each p

Check if p is true (or false) after OP

```
Q: When is p true after OP?
```

- If WP(p, OP) is true before OP!
- We know F is true before OP_
- Thm. Pvr. Query: $F \Rightarrow WP(p, OP)$

How to compute successor?

```
Example ( ) {
    1: do{
        lock();
        old = new;
        q = q->next;

2: if (q != NULL) {
    3:        q->data = new;
        unlock();
        new ++;
    }

4:}while(new != old);

5: unlock ();
}
```

```
LOCK, new==old 3 F
OP
4 ?
```

For each p

Check if p is true (or false) after OP

```
Q: When is p false after OP?
```

- If $WP(\neg p, OP)$ is true <u>before</u> OP!
- We know F is true before OP_
- Thm. Pvr. Query: $F \Rightarrow WP(\neg p, OP)$

How to compute successor?

```
Example ( ) {
    1: do{
        lock();
        old = new;
        q = q->next;

2: if (q != NULL) {
    3:        q->data = new;
        unlock();
        new ++;
    }

4:}while(new != old);

5: unlock ();
}
```

```
LOCK, new==old 3 F

OP

- LOCK, ¬ new = old 4?
```

For each p

Check if p is true (or false) after OP

```
Q: When is p false <u>after OP</u>?
- If WP(¬p, OP) is true <u>before OP</u>!
- We know F is true <u>before OP</u>_
- Thm. Pvr. Query: F ⇒ WP(¬p, OP)
```

```
Predicate: new==old
```

```
True ? (LOCK, new==old) \Rightarrow (new + 1 = old) NO
False ? (LOCK, new==old) \Rightarrow (new + 1 \neq old) YES
```

Advanced SLAM/BLAST

Too Many Predicates

- Use Predicates Locally

Counter-Examples

- Craig Interpolants

Procedures

- Summaries

Concurrency

- Thread-Context Reasoning

SLAM Summary

- 1) Instrument Program With Safety Policy
- 2) Predicates = { }
- 3) Abstract Program With Predicates
 - Use Weakest Preconditions and Theorem Prover Calls
- 4) Model-Check Resulting Boolean Program
 - Use Symbolic Model Checking
- 5) Error State Not Reachable?
 - Original Program Has No Errors: Done!
- 6) Check Counterexample Feasibility
 - Use Symbolic Execution
- 7) Counterexample Is Feasible?
 - Real Bug: Done!
- 8) Counterexample Is Not Feasible?
 - 1) Find New Predicates (Refine Abstraction)
 - 2) Goto Line 3

Optional: SLAM Weakness

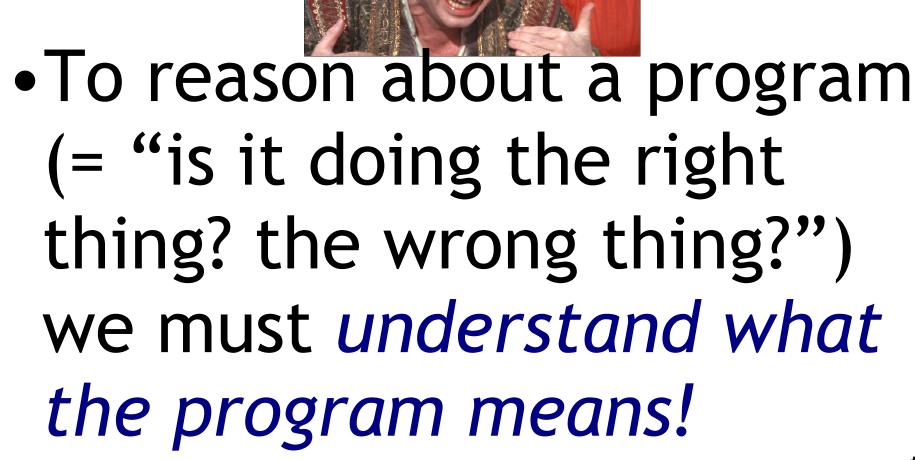
```
1: F() {
2: int x=0;
3: lock();
4: do x++;
5: while (x \neq 88);
6: if (x < 77)
7: lock();
8: }
```

- Preds = {}, Path = 234567
- $[x=0, \neg x+1\neq 88, x+1<77]$
- Preds = $\{x=0\}$, Path = 234567
- $[x=0, \neg x+1\neq 88, x+1<77]$
- Preds = $\{x=0, x+1=88\}$
- Path = 23454567
- $[x=0, \neg x+2\neq 88, x+2<77]$
- Preds = $\{x=0,x+1=88,x+2=88\}$
- Path = 2345454567
- ...
- Result: the predicates "count" the loop iterations

Lessons From Model Checking

- To find bugs, we need specifications
 - What are some good specifications?
- To convert a program into a model, we need predicates/invariants and a theorem prover.
 - What are important predicates? Invariants?
 - What should we track when reasoning about a program and what should we abstract?
 - How does a theorem prover work?
- Simple algorithms (e.g., depth first search, pushing facts along a CFG) can work well
 - ... under what circumstances?

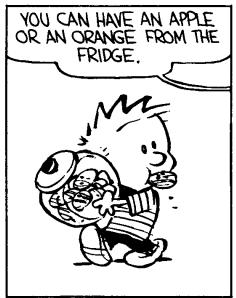
The Big Lesson



A Simple Imperative Language Operational Semantics (= "meaning")





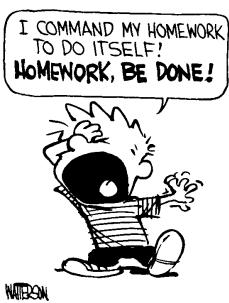




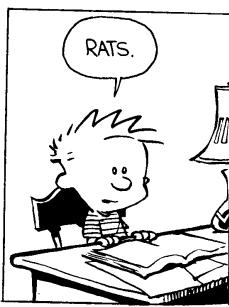
Homework #1 Out Today

- Due One Week From Now
- Take a look tonight
- My office hours are Fridays at this time









Medium-Range Plan

- Study a simple imperative language IMP
 - Abstract syntax (today)
 - Operational semantics (today)
 - Denotational semantics
 - Axiomatic semantics
 - ... and relationships between various semantics (with proofs, peut-être)
 - Today: operational semantics
 - Follow along in Chapter 2 of Winskel

Syntax of IMP

- Concrete syntax: The rules by which programs can be expressed as strings of characters
 - Keywords, identifiers, statement separators vs. terminators (Niklaus!?), comments, indentation (Guido!?)
- Concrete syntax is important in practice
 - For readability (Larry!?), familiarity, parsing speed (Bjarne!?), effectiveness of error recovery, clarity of error messages (Robin!?)
- Well-understood principles
 - Use finite automata and context-free grammars
 - Automatic lexer/parser generators

(Note On Recent Research)

- If-as-and-when you find yourself making a new language, consider GLR (elkhound) instead of LALR(1) (bison)
- Scott McPeak, George G. Necula: Elkhound: A Fast, Practical GLR Parser Generator. CC 2004: pp. 73-88
- As fast as LALR(1), more natural, handles basically all of C++, etc.

Abstract Syntax

- We ignore parsing issues and study programs given as abstract syntax trees
 - I provide the parser in the homework ...
- An abstract syntax tree is (a subset of) the parse tree of the program
 - Ignores issues like comment conventions
 - More convenient for formal and algorithmic manipulation
 - All research papers use ASTs, etc.

IMP Abstract Syntactic Entities

- int integer constants ($n \in \mathbb{Z}$)
- bool bool constants (true, false)
 - locations of variables (x, y)
- Aexp arithmetic expressions (e)
- Bexp boolean expressions (b)
- Com commands (c)

- (these also encode the types)

Abstract Syntax (Aexp)

Arithmetic expressions (Aexp)

```
e::= n for n \in \mathbb{Z}

| x for x \in L

| e_1 + e_2 for e_1, e_2 \in Aexp

| e_1 - e_2 for e_1, e_2 \in Aexp

| e_1 * e_2 for e_1, e_2 \in Aexp
```

Notes:

- Variables are not declared
- All variables have integer type
- No side-effects (in expressions)

Abstract Syntax (Bexp)

• Boolean expressions (Bexp)

```
b ::= true
       I false
                              for e_1, e_2 \in Aexp
       | e_1 = e_2
                              for e_1, e_2 \in Aexp
       | e_1 \le e_2
       I - b
                              for b \in Bexp
       |b_1 \wedge b_2|
                              for b_1, b_2 \in Bexp
                              for b_1, b_2 \in Bexp
       |b_1 \vee b_2|
```

"Boolean"

- George Boole
 - 1815-1864
- I'll assume you know boolean algebra ...

p	q	$p \wedge q$
T	T	T
T	F	F
F	T	F
F	F	F



Abstract Syntax (Com)



Commands (Com)

```
c::= skip

| x := e  x \in L \land e \in Aexp

| c_1 ; c_2  c_1, c_2 \in Com

| if b then c_1 else c_2  c_1, c_2 \in Com \land b \in Bexp

| while b do c c \in Com \land b \in Bexp
```

• Notes:

- The typing rules are embedded in the syntax definition
- Other parts are not context-free and need to be checked separately (e.g., all variables are declared)
- Commands contain all the side-effects in the language
- Missing: pointers, function calls, what else?

Why Study Formal Semantics?

- Language design (denotational)
- Proofs of correctness (axiomatic)
- Language implementation (operational)
- Reasoning about programs
- Providing a clear behavioral specification
- "All the cool people are doing it."
 - You need this to understand PL research
- "First one's free."

Consider This Java

```
x = 0;
try {
 x = 1;
 break mygoto;
} finally {
 x = 2;
 raise
  NullPointerException;
x = 3;
mygoto:
```

- What happens when you execute this code?
- Notably, what assignments are executed?

14.20.2 Execution of try-catch-finally

- A try statement with a finally block is executed by first executing the try block. Then there is a choice:
- If execution of the try block completes normally, then the finally block is executed, and then there is a choice:
 - If the finally block completes normally, then the try statement completes normally.
 - If the finally block completes abruptly for reason S, then the try statement completes abruptly for reason S.
- If execution of the try block completes abruptly because of a throw of a value V, then there is a choice:
 - If the run-time type of V is assignable to the parameter of any catch clause of the try statement, then the first (leftmost) such catch clause is selected. The value V is assigned to the parameter of the selected catch clause, and the *Block* of that catch clause is executed. Then there is a choice:
 - If the catch block completes normally, then the finally block is executed. Then there is a choice:
 - If the finally block completes normally, then the try statement completes normally.
 - If the finally block completes abruptly for any reason, then the try statement completes abruptly for the same reason.
 - If the catch block completes abruptly for reason R, then the finally block is executed. Then there is a choice:
 - If the finally block completes normally, then the try statement completes abruptly for reason R.
 - If the finally block completes abruptly for reason S, then the try statement completes abruptly for reason S (and reason R is discarded).
 - If the run-time type of V is not assignable to the parameter of any catch clause of the try statement, then the finally block is executed. Then there is a choice:
 - If the finally block completes normally, then the try statement completes abruptly because of a throw of the value
 - If the finally block completes abruptly for reason S, then the try statement completes abruptly for reason S (and the throw of value V is discarded and forgotten).
- If execution of the try block completes abruptly for any other reason R, then the finally block is executed. Then there is a choice:
 - If the finally block completes normally, then the try statement completes abruptly for reason R.
 - If the finally block completes abruptly for reason S, then the try statement completes abruptly for reason S (and reason R is discarded).



Ouch! Confusing.

- Wouldn't it be nice if we had some way of describing what a language (feature or program) means ...
 - More precisely than English
 - More compactly than English
 - So that you might build a compiler
 - So that you might prove things about programs

Analysis of IMP

- Questions to answer:
 - What is the "meaning" of a given IMP expression/command?
 - How would we go about evaluating IMP expressions and commands?
 - How are the evaluator and the meaning related?

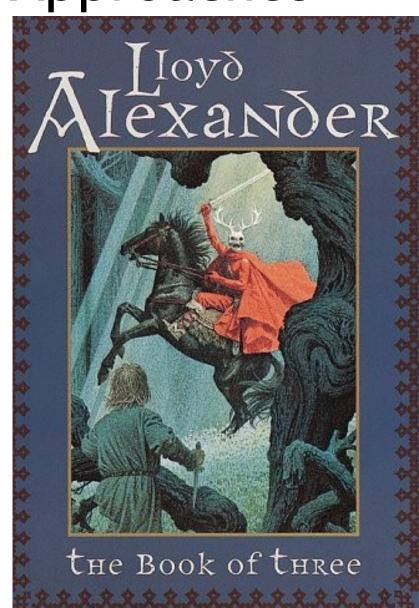
Three Canonical Approaches

Operational

- How would I execute this?
- "Symbolic Execution"

Axiomatic

- What is true after I execute this?
- Denotational
 - What is this trying to compute?



An Operational Semantics

- Specifies how expressions and commands should be evaluated
- Depending on the form of the expression
 - 0, 1, 2, . . . don't evaluate any further.
 - They are <u>normal forms</u> or <u>values</u>.
 - $e_1 + e_2$ is evaluated by first evaluating e_1 to n_1 , then evaluating e_2 to n_2 . (post-order traversal)
 - The result of the evaluation is the literal representing $n_1 + n_2$.
 - Similarly for e₁ * e₂
- Operational semantics abstracts the execution of a concrete interpreter
 - Important keywords are colored & underlined in this class.

Semantics of IMP

- The meanings of IMP expressions depend on the values of variables
 - What does "x+5" mean? It depends on "x"!
- The value of variables at a given moment is abstracted as a function from L to Z (a <u>state</u>)
 - If x 8 in our state, we expect "x+5" to mean 13
- The set of all states is $\Sigma = L \rightarrow \mathbb{Z}$
- We shall use σ to range over Σ
 - σ , a state, maps variables to values

Notation: Judgment

• We write:

- To mean that e evaluates to n in state σ .
- This is a judgment. It asserts a relation between e, σ and n.
- In this case we can view \downarrow as a function with two arguments (e and σ).

Operational Semantics

- This formulation is called <u>natural</u> <u>operational semantics</u>
 - or big-step operational semantics
 - the ↓ judgment relates the expression and its "meaning"

How should we define

$$\langle e_1 + e_2, \sigma \rangle \downarrow \dots ?$$

Notation: Rules of Inference

- We express the evaluation rules as <u>rules of</u> <u>inference</u> for our judgment
 - called the <u>derivation rules</u> for the judgment
 - also called the <u>evaluation rules</u> (for operational semantics)
- In general, we have one rule for each language construct:

$$\langle e_1, \sigma \rangle \downarrow n_1 \quad \langle e_2, \sigma \rangle \downarrow n_2$$
This is the only rule for $e_1 + e_2$

Rules of Inference

Hypothesis₁ ... Hypothesis_N

Conclusion

```
\Gamma \vdash b : bool \quad \Gamma \vdash e1 : \tau \quad \Gamma \vdash e2 : \tau
```

 $\Gamma \vdash$ if b then e1 else e2 : τ

- For any given proof system, a finite number of rules of inference (or schema) are listed somewhere
- Rule instances should be easily checked
- What is the definition of "NP"?

Derivation

$$\frac{\Gamma(x)=int}{\Gamma\vdash x:int} \text{ var } \frac{\Gamma(x)=int}{\Gamma\vdash x:int} \text{ sub } \frac{\Gamma\vdash x:int}{\Gamma\vdash x:int} \text{ sub } \frac{\Gamma\vdash x:int}{\Gamma\vdash x:int} \text{ assign } \frac{\Gamma\vdash x:int}{\Gamma\vdash x:int} \text{ of } \frac{\Gamma\vdash x:int}{\Gamma\vdash x:int} \text{$$

- Tree-structured (conclusion at bottom)
- May include multiple sorts of rules-ofinference
- Could be constructed, typically are not
- Typically verified in polynomial time

Evaluation Rules (for Aexp)

- This is called <u>structural operational semantics</u>
 - rules defined based on the structure of the expression
- These rules do not impose an order of evaluation!

Evaluation Rules (for Bexp)

(show: candidate ∨ rule)

How to Read the Rules?

- Forward (top-down) = inference rules
 - if we know that the hypothesis judgments hold then we can infer that the conclusion judgment also holds

- If we know that $\langle e_1, \sigma \rangle \downarrow 5$ and $\langle e_2, \sigma \rangle \downarrow 7$, then we can infer that $\langle e_1 + e_2, \sigma \rangle \downarrow 12$

How to Read the Rules?

- Backward (bottom-up) = evaluation rules
 - Suppose we want to evaluate $e_1 + e_2$, i.e., find $n \text{ s.t. } e_1 + e_2 \downarrow n$ is derivable using the previous rules
 - By inspection of the rules we notice that the last step in the derivation of $e_1 + e_2 \Downarrow n$ must be the addition rule
 - the other rules have conclusions that would not match $e_1 + e_2 \downarrow n$
 - this is called reasoning by <u>inversion</u> on the derivation rules

Evaluation By Inversion

- Thus we must find n_1 and n_2 such that \downarrow n_1 and $e_2 \downarrow n_2$ are derivable
 - This is done recursively
- If there is exactly one rule for each kind of expression we say that the rules are <u>syntax-directed</u>
 - At each step at most one rule applies
 - This allows a simple evaluation procedure as above (recursive tree-walk)
 - True for our Aexp but not Bexp. Why?

Evaluation of Commands

- The evaluation of a Com may have side effects but has no direct result
 - What is the result of evaluating a command?
- The "result" of a Com is a new state:

- But the evaluation of Com might not terminate! Danger Will Robinson! (huh?)



Com Evaluation Rules 1

$$\frac{\langle c_1, \sigma \rangle \Downarrow \sigma' \quad \langle c_2, \sigma' \rangle \Downarrow \sigma''}{\langle c_1; c_2, \sigma \rangle \Downarrow \sigma''}$$

$$\frac{\langle b, \sigma \rangle \Downarrow \text{true} \quad \langle c_1, \sigma \rangle \Downarrow \sigma'}{\langle \text{if b then } c_1 \text{ else } c_2, \sigma \rangle \Downarrow \sigma'}$$

$$\frac{\langle b, \sigma \rangle \Downarrow \text{false} \quad \langle c_2, \sigma \rangle \Downarrow \sigma'}{\langle \text{if b then } c_1 \text{ else } c_2, \sigma \rangle \Downarrow \sigma'}$$

Com Evaluation Rules 2

$$\langle e, \sigma \rangle \downarrow n$$
 Def: $\sigma[x:=n](x) = n$ $\sigma[x:=n](y) = \sigma(y)$

Let's do while together

Com Evaluation Rules 3

$$↓ n$$
 $↓ σ[x := n]$

Def:
$$\sigma[x:=n](x) = n$$

 $\sigma[x:=n](y) = \sigma(y)$

$$<$$
b, $σ$ > $↓$ false

<while b do c, σ > ψ σ

b, σ>
$$\Downarrow$$
 true \Downarrow σ'

<while b do c, $\sigma > \psi \sigma'$

Homework

- Homework 1 Out Today
 - Due In One Week
- Read at least 1 of these 3 Articles
 - 1. Wegner's *Programming Languages The First 25* years
 - 2. Wirth's On the Design of Programming Languages
 - 3. Nauer's Report on the algorithmic language ALGOL 60
- Skim the optional reading we'll discuss opsem "in the wild" next time