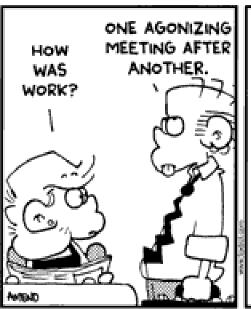
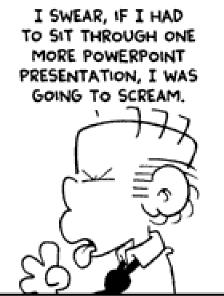
Lexical Analysis

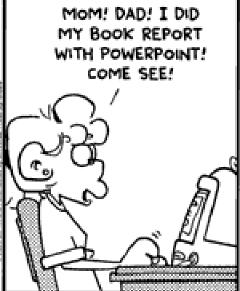
Finite Automata

(Part 2 of 2)



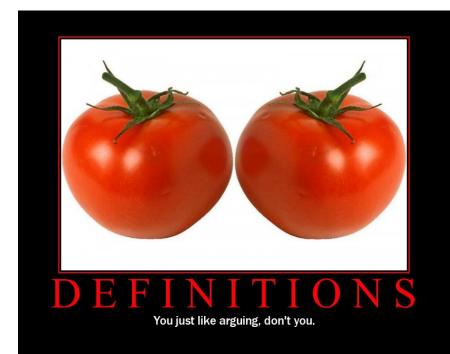






PAO, PA1

- Although we have included the tricky "file ends without a newline" testcases in previous years, students made good cases against them (e.g., they test I/O and not the algorithm) so we are dropping them from PA1.
- You can submit new rosetta.yada files for PA1, so you can fix errors from PA0.

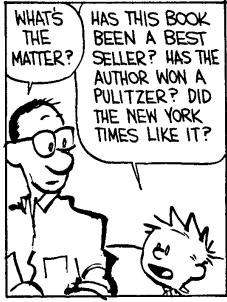




Reading Quiz!

- Are practical parsers and scanners based on deterministic or non-deterministic automata?
- How can regular expressions be used to specify nested constructs?
- How is a two-dimensional transition table used in tabledriven scanning?









Credits

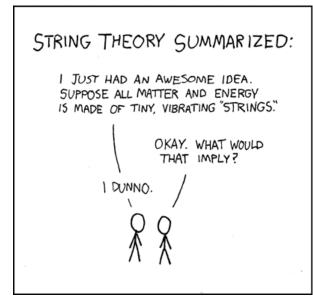
- The majority of you (25/31) are signed up for 2 credits of CS 4993-04
 - Do a big Compiler project, attend "Discussion Section", get 5 credits total
 - Similar to Cornell's approach, etc.
- How many of you are planning to take Compilers?
 - Odds are "50-50" it will be offered in the Spring
 - Don't take Compilers if you're taking 5 credits here
- Don't want five credits / will take Compilers?
 - Come see me in person, we'll work something out.
 - Different assignment list, etc.

Cunning Plan

Regular expressions provide a concise

notation for string patterns

- Use in lexical analysis requires extensions
 - To resolve ambiguities
 - To handle errors
- Good algorithms known (next)
 - Require only single pass over the input
 - Few operations per character (table lookup)



One-Slide Summary

- Finite automata are formal models of computation that can accept regular languages corresponding to regular expressions.
- Nondeterministic finite automata (NFA)
 feature epsilon transitions and multiple
 outgoing edges for the same input symbol.
- Regular expressions can be converted to NFAs.
- Tools will generate DFA-based lexer code for you from regular expressions.

Finite Automata

- Regular expressions = specification
- Finite automata = implementation

- A finite automaton consists of
 - An input alphabet ∑
 - A set of states \$
 - A start state n
 - A set of accepting states F ⊆ S
 - A set of transitions state → input state

Finite Automata

Transition

$$S_1 \rightarrow^a S_2$$

Is read

In state s₁ on input "a" go to state s₂

- If end of input (or no transition possible)
 - If in accepting state ⇒ accept
 - Otherwise ⇒ reject

Finite Automata State Graphs

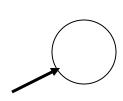
A state

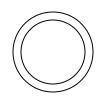


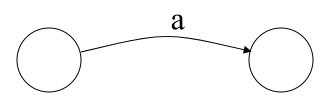
An accepting state

A transition



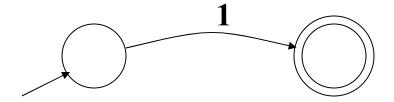






A Simple Example

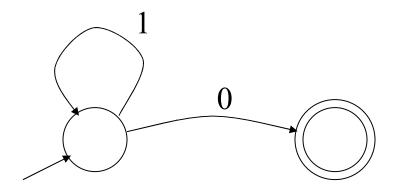
A finite automaton that accepts only "1"



 A finite automaton <u>accepts</u> a string if we can follow transitions labeled with the characters in the string from the start to some accepting state

Another Simple Example

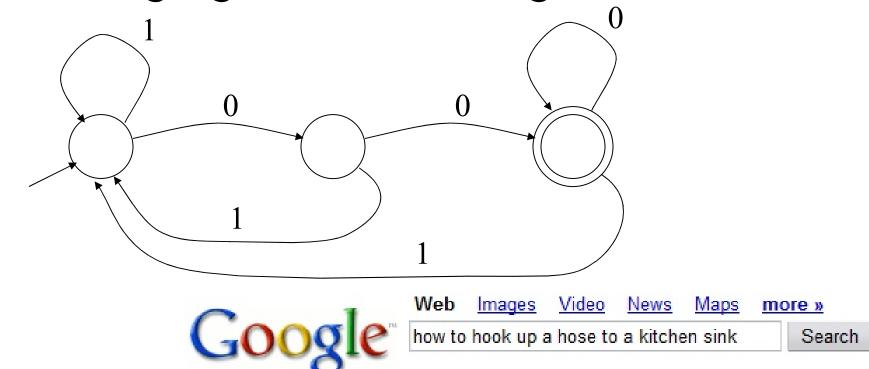
- A finite automaton accepting any number of 1's followed by a single 0
- Alphabet $\Sigma = \{0,1\}$



 Check that "1110" is accepted but "110..." is not

And Another Example

- Alphabet $\Sigma = \{0,1\}$
- What language does this recognize?

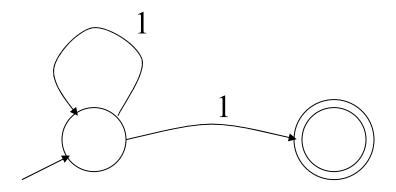


Web

Did you mean: how to hook up a horse to a kitchen sink

And Another Example

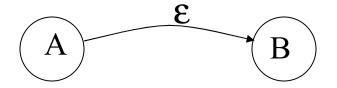
• Alphabet still $\Sigma = \{0, 1\}$



- The operation of the automaton is not completely defined by the input
 - On input "11" the automaton could be in either state

Epsilon Moves

• Another kind of transition: ε-moves



Machine can move from state A to state B

without reading input



Deterministic and Nondeterministic Automata

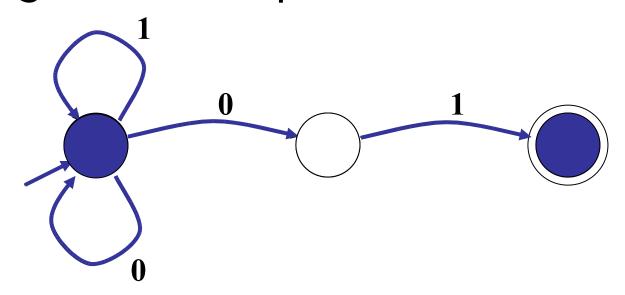
- Deterministic Finite Automata (DFA)
 - One transition per input per state
 - No ε-moves
- Nondeterministic Finite Automata (NFA)
 - Can have multiple transitions for one input in a given state
 - Can have ε-moves
- Finite automata have finite memory
 - Need only to encode the current state

Execution of Finite Automata

- A DFA can take only one path through the state graph
 - Completely determined by input
- NFAs can choose
 - Whether to make ε-moves
 - Which of multiple transitions for a single input to take

Acceptance of NFAs

An NFA can get into multiple states



- Input: 1 0 1
- Rule: NFA accepts if it <u>can</u> get in a final state

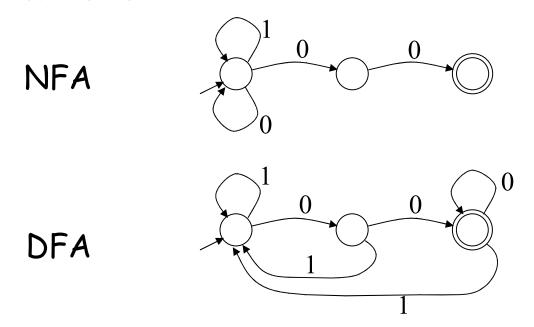
NFA vs. DFA (1)

- NFAs and DFAs recognize the same set of languages (regular languages)
 - They have the same expressive power
- DFAs are easier to implement
 - There are no choices to consider



NFA vs. DFA (2)

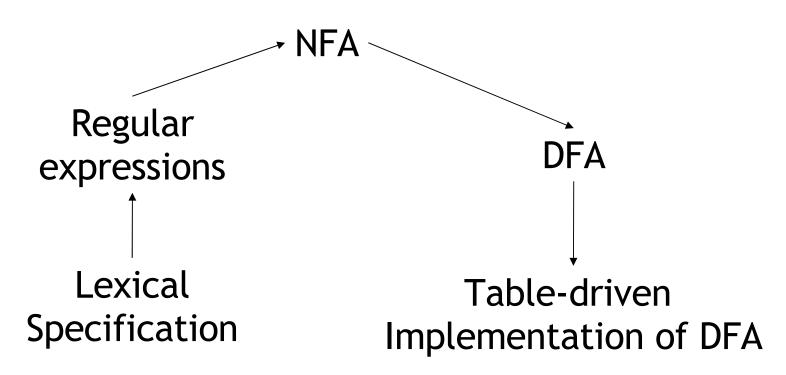
 For a given language the NFA can be simpler than the DFA



DFA can be exponentially larger than NFA

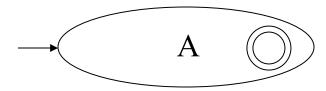
Regular Expressions to Finite Automata

High-level sketch

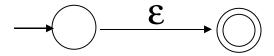


Regular Expressions to NFA (1)

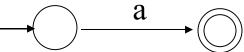
- For each kind of rexp, define an NFA
 - Notation: NFA for rexp A



• For ε

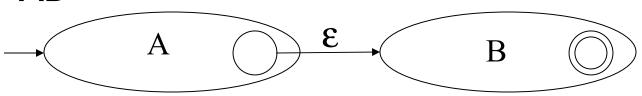


For input a

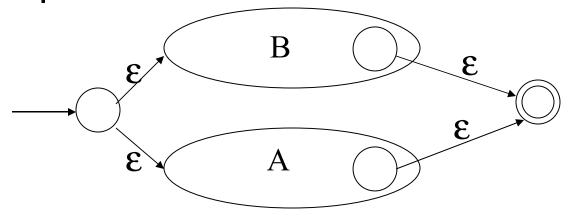


Regular Expressions to NFA (2)

For AB

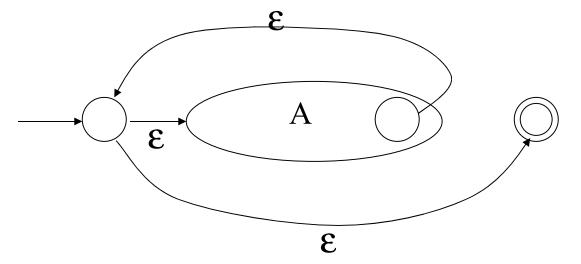


• For A | B



Regular Expressions to NFA (3)

For A*









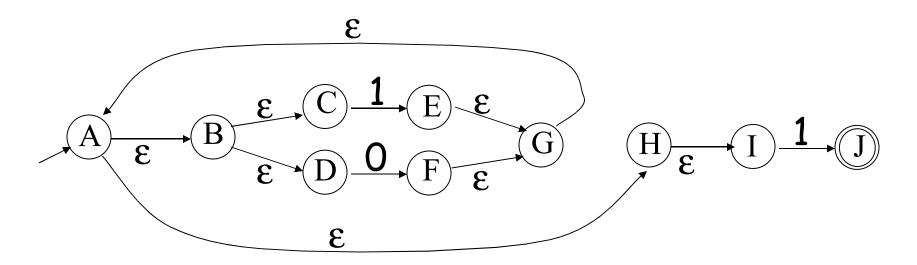


Example of RegExp -> NFA Conversion

Consider the regular expression

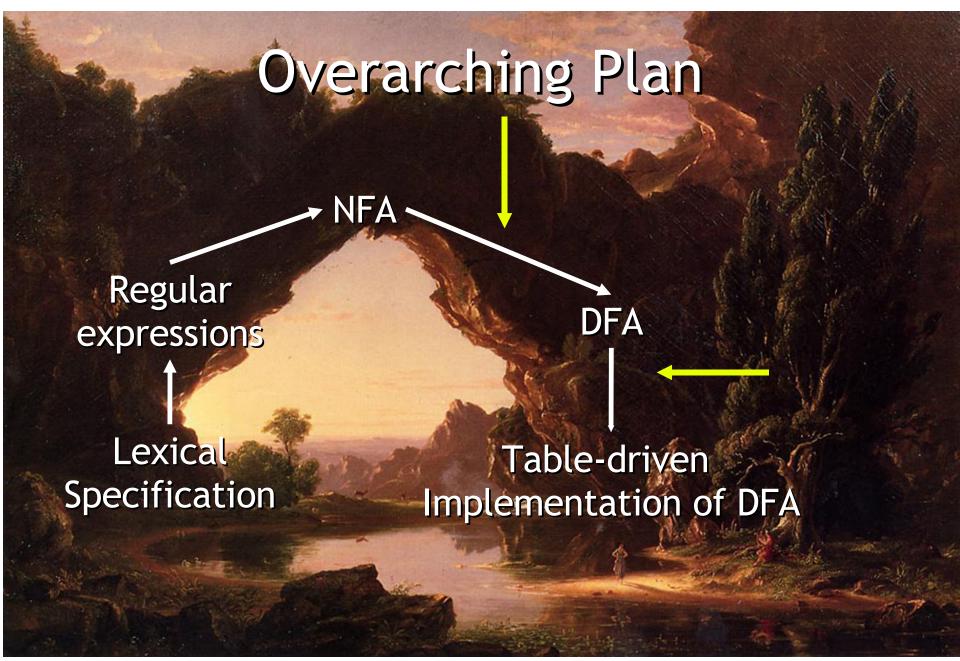
$$(1 | 0)* 1$$

The NFA is



Break Time

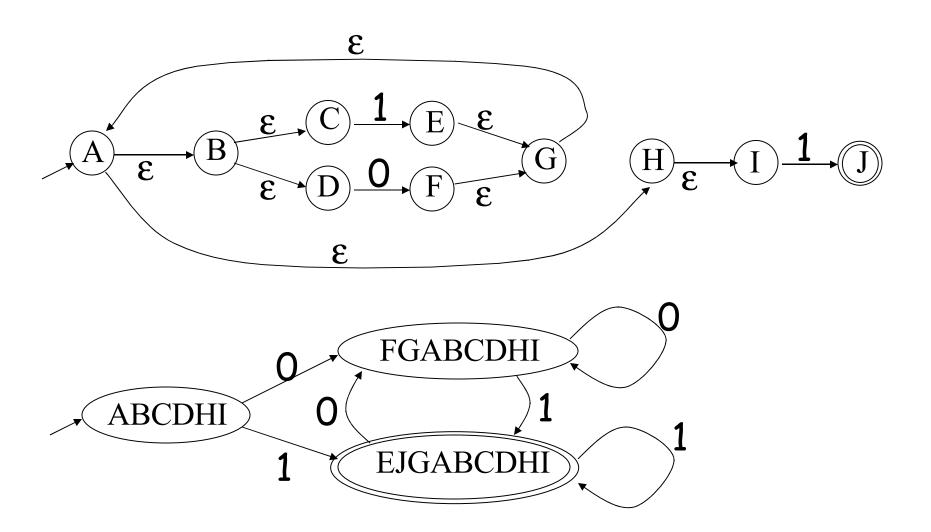
- Students pick numbers 1-454 for
- http://www.cs.virginia.edu/~weimer/english.html
- Start with 381 if you lake a PRNG ...



NFA to DFA: The Trick

- Simulate the NFA
- Each state of DFA
 - = a non-empty *subset of states* of the NFA
- Start state
 - = the set of NFA states reachable through ϵ -moves from NFA start state
- Add a transition $S \rightarrow a S'$ to DFA iff
 - S' is the set of NFA states reachable from the states in S after seeing the input a
 - considering ϵ -moves as well

NFA → DFA Example



NFA → DFA: Remark

An NFA may be in many states at any time

How many different states?

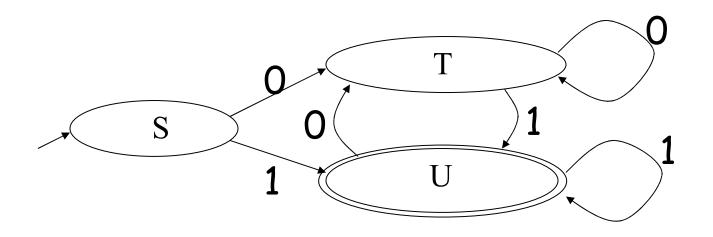
 If there are N states, the NFA must be in some subset of those N states

- How many non-empty subsets are there?
 - 2^N 1 = finitely many

Implementation

- A DFA can be implemented by a 2D table T
 - One dimension is "states"
 - Other dimension is "input symbols"
 - For every transition $S_i \rightarrow^a S_k$ define T[i,a] = k
- DFA "execution"
 - If in state S_i and input a, read T[i,a] = k and skip to state S_k
 - Very efficient

Table Implementation of a DFA



	0	1
S	Τ	U
Τ	Τ	U
٦	Τ	J

Implementation (Cont.)

 NFA → DFA conversion is at the heart of tools such as flex or ocamllex

But, DFAs can be huge

 In practice, flex-like tools trade off speed for space in the choice of NFA and DFA representations

PA2: Lexical Analysis

Tip of the Day

Did you know...

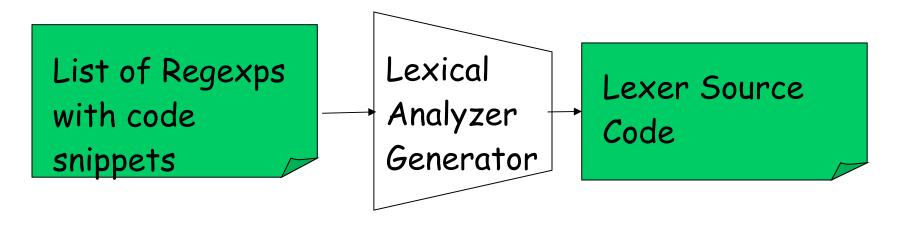
Correctness is job #1.



- Tips on building large systems:
 - Keep it simple
 - Design systems that can be tested
 - Don't optimize prematurely
 - It is easier to modify a working system than to get a system working

Lexical Analyzer Generator

- Tools like lex and flex and ocamllex will build lexers for you!
- You will use this for PA2



- I'll explain ocamllex; others are similar
 - See PA2 documentation

Ocamllex "lexer.mll" file

```
(* raw preamble code
      type declarations, utility functions, etc. *)
let re_name; = re;
rule normal_tokens = parse
  re<sub>1</sub> { token<sub>1</sub> }
  re, { token, }
and special, okens = parse
  re<sub>n</sub> { token<sub>n</sub> }
```

Example "lexer.mll"

```
type token = Tok_Integer of int
                                        (* 123 *)
                                        (* / *)
       | Tok_Divide
let digit = ['0' - '9']
rule initial = parse
             { Tok_Divide }
| digit digit* { let token_string = Lexing.lexeme lexbuf in
              let token_val = int_of_string token_string in
              Tok_Integer(token_val) }
             { Printf.printf "Error!\n"; exit 1 }
```

Adding Winged Comments

```
type token = Tok_Integer of int
                                     (* 123 *)
        | Tok_Divide
let digit = ['0' - '9']
rule initial = parse
  "//" { eol_comment } (* why am I the "first" rule? *)
             { Tok_Divide }
 digit digit* { let token_string = Lexing.lexeme lexbuf in
                let token_val = int_of_string token_string in
                Tok_Integer(token_val) }
               { Printf.printf "Error!\n"; exit 1 }
and eol_comment = parse
 '\n' { initial lexbuf }
      { eol_comment lexbuf }
```

Using Lexical Analyzer Generators

\$ ocamllex lexer.mll

```
45 states, 1083 transitions, table size 4602 bytes
(* your main.ml file ... *)
let file_input = open_in "file.cl" in
let lexbuf = Lexing.from_channel file_input in
let token = Lexer, initial lexbuf in
match token with
| Tok_Divide -> printf "Divide Token!\n"
| Tok_Integer(x) -> printf "Integer Token = %d\n" x
```

How Big Is PA2?

- The reference "lexer.mll" file is 88 lines
 - Perhaps another 20 lines to keep track of input line numbers
 - Perhaps another 20 lines to open the file and get a list of tokens
 - Then 65 lines to serialize the output
 - I'm sure it's possible to be smaller!

• Conclusion:

- This isn't a code slog, it's about careful forethought and precision.

Think about: quoted strings!

Homework

- Wednesday: PA1 due
- Thursday: Chapters 2.4 2.4.1 (on website)