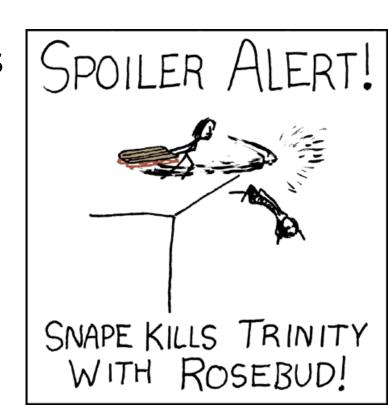


Outline

Review of bottom-up parsing

- Computing the parsing DFA
 - Closures, LR(1) Items, States
 - Transitions

- Using parser generators
 - Handling Conflicts



In One Slide

 An LR(1) parsing table can be constructed automatically from a CFG. An LR(1) item is a pair made up of a production and a lookahead token; it represents a possible parser context. After we extend LR(1) items by closing them they become LR(1) DFA states. Grammars can have shift/reduce or reduce/reduce conflicts. You can fix most conflicts with precedence and associativity declarations. LALR(1) tables are formed from LR(1) tables by merging states with similar cores.

Bottom-up Parsing (Review)

- A bottom-up parser rewrites the input string to the start symbol
- The state of the parser is described as

$$\alpha \triangleright \gamma$$

- α is a stack of terminals and non-terminals
- γ is the string of terminals not yet examined

• Initially: $\rightarrow x_1 x_2 \dots x_n$

Shift and Reduce Actions (Review)

- Recall the CFG: $E \rightarrow int \mid E + (E)$
- A bottom-up parser uses two kinds of actions:
- Shift pushes a terminal from input on the stack

$$E + (\triangleright int) \Rightarrow E + (int \triangleright)$$

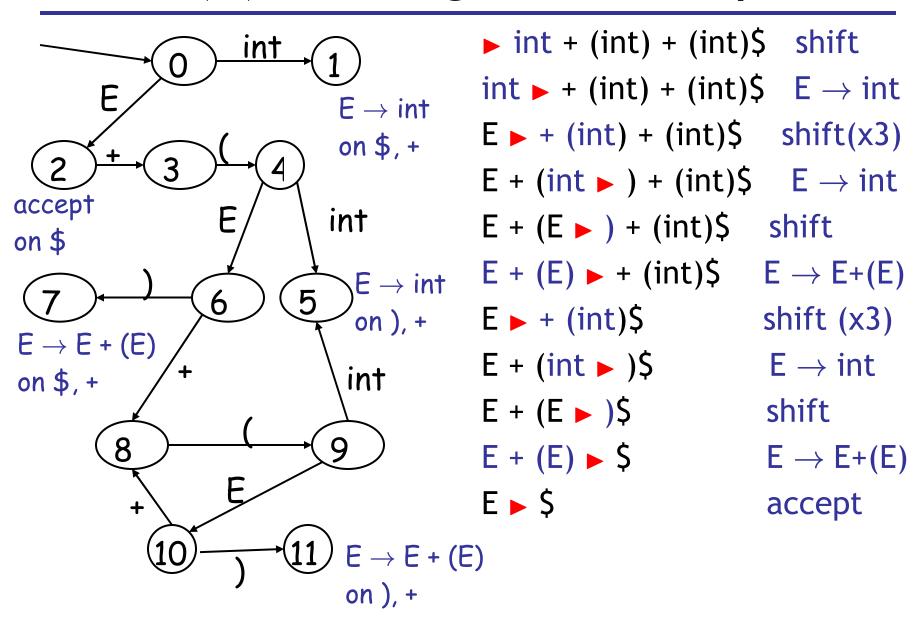
 Reduce pops 0 or more symbols off of the stack (production RHS) and pushes a non-terminal on the stack (production LHS)

$$E + (\underline{E} + (\underline{E}) \rightarrow) \Rightarrow E + (\underline{E} \rightarrow)$$

Key Issue: When to Shift or Reduce?

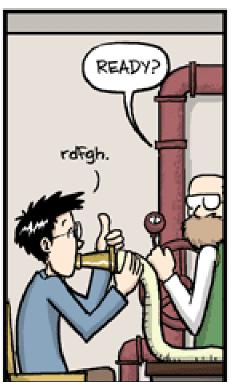
- Idea: use a finite automaton (DFA) to decide when to shift or reduce
 - The input is the stack
 - The language consists of terminals and non-terminals
- We run the DFA on the stack and we examine the resulting state X and the token tok after ►
 - If X has a transition labeled tok then shift
 - If X is labeled with " $A \rightarrow \beta$ on tok" then reduce

LR(1) Parsing. An Example



End of review





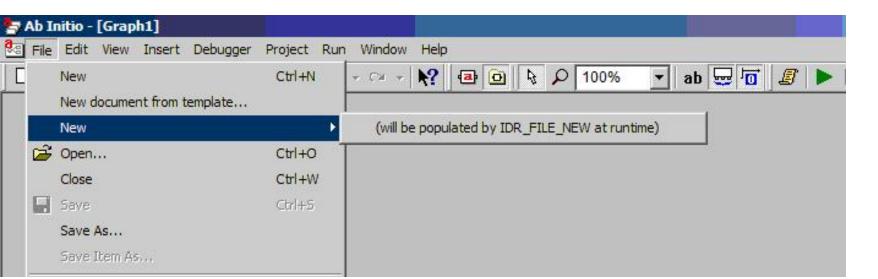




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Key Issue: How is the DFA Constructed?

- The stack describes the context of the parse
 - What non-terminal we are looking for
 - What production rhs we are looking for
 - What we have seen so far from the rhs



$$\int \frac{b dx}{(x-a)^2 + b^2} = \int \frac{dx}{b} \cos^2 \theta = \int d\theta$$

$$d(\tan \theta) = \Delta e^{\frac{1}{2}} \theta d\theta = \frac{d\theta}{\cos^2 \theta}$$

$$= d(\frac{x-a}{b}) = \frac{dx}{b}$$

$$\int \frac{b dx}{(x-a)^2 + b^2} = \int d \left[\tan^2(\frac{x-a}{b}) \right]$$
The integral is bounded from below, but not from above
$$\int_0^{\infty} \frac{b dx}{(x-a)^2 + b^2} = \int_{x=0}^{x=\infty} d \left[\tan^2(\frac{x-a}{b}) \right] = \int_{x=0}^{x=0} d \left[\tan^2(\frac{x-a}{b}) \right] = \int_{x=0}^{x=\infty} d \left[\tan^2(\frac{x-a}{b}) \right] = \int_{x=0}^{x=\infty} d \left[\tan^2(\frac{x-a}{b}) \right] = \int_{x=0}^{x=\infty} d \left[\tan^$$

LR(1) Table Construction

Three hours later, you can finally parse $E \rightarrow E + E \mid int$

Parsing Contexts

• Consider the state:

```
E
/
int + ( int ) + ( int )
```

- The stack is

Red dot =

where we are.

- Context:
 - We are looking for an $E \rightarrow E + (\bullet E)$
 - Have have seen E + (from the right-hand side
 - We are also looking for $E \rightarrow \bullet$ int or $E \rightarrow \bullet E + (E)$
 - Have seen nothing from the right-hand side
- One DFA state must thus describe <u>several</u> contexts

LR(1) Items

• An LR(1) item is a pair:

$$X \rightarrow \alpha \bullet \beta$$
, a

- $X \rightarrow \alpha \beta$ is a production
- a is a terminal (the lookahead terminal)
- LR(1) means 1 lookahead terminal
- $[X \rightarrow \alpha \bullet \beta, a]$ describes a context of the parser
 - We are trying to find an X followed by an a, and
 - We have α already on top of the stack
 - Thus we need to see next a prefix derived from βa

Note

- The symbol > was used before to separate the stack from the rest of input
 - $\alpha \triangleright \gamma$, where α is the stack and γ is the remaining string of terminals
- In LR(1) items is used to mark a prefix of a production rhs:

$$X \rightarrow \alpha \bullet \beta$$
, a

- Here β might contain non-terminals as well
- In both case the stack is on the left

Convention

- We add to our grammar a fresh new start symbol S and a production $S \rightarrow E$
 - Where E is the old start symbol
 - No need to do this if E had only one production
- The initial parsing context contains:

$$S \rightarrow \bullet E, $$$

- Trying to find an S as a string derived from E\$
- The stack is empty

LR(1) Items (Cont.)

In context containing

$$\mathsf{E} \to \mathsf{E} + \bullet (\mathsf{E}), +$$

 If (follows then we can perform a shift to context containing

$$\mathsf{E} \to \mathsf{E} + (\bullet \mathsf{E}), +$$

In context containing

$$\mathsf{E} \to \mathsf{E} + (\mathsf{E}) \bullet, +$$

- We can perform a reduction with $E \rightarrow E + (E)$
- But only if a + follows

LR(1) Items (Cont.)

Consider a context with the item

$$E \rightarrow E + (\bullet E), +$$

- We expect next a string derived from E) +
- There are two productions for E

$$E \rightarrow int$$
 and $E \rightarrow E + (E)$

 We describe this by extending the context with two more items:

$$E \rightarrow \bullet \text{ int, })$$
 $E \rightarrow \bullet E + (E),)$

The Closure Operation

 The operation of extending the context with items is called the closure operation

```
Closure(Items) =
  repeat
     for each [X \rightarrow \alpha \bullet Y\beta, a] in Items
         for each production Y \rightarrow \gamma
              for each b \in First(\beta a)
                  add [Y \rightarrow \bullet \gamma, b] to Items
  until Items is unchanged
```

Constructing the Parsing DFA (1)

Construct the start context:

Closure(
$$\{S \to \bullet E, \$\}$$
) = $S \to \bullet E, \$$
 $E \to \bullet E+(E), \$$
 $E \to \bullet int, \$$
• We abbreviate as: $E \to \bullet int, +$
 $S \to \bullet E, \$$
 $E \to \bullet E+(E), \$/+$
 $E \to \bullet int, \$/+$



PLANNING

You... have a plan, right?

Constructing the Parsing DFA (2)

- An LR(1) DFA state is a closed set of LR(1) items
 - This means that we performed Closure
- The start state contains [S → •E, \$]
- A state that contains $[X \rightarrow \alpha \bullet, b]$ is labeled with "reduce with $X \rightarrow \alpha$ on b"

And now the transitions ...

The DFA Transitions

- A state "State" that contains $[X \to \alpha \bullet y\beta, b]$ has a transition labeled y to a state that contains the items "Transition(State, y)"
 - y can be a terminal or a non-terminal

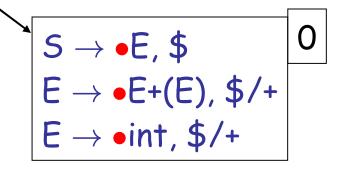
```
Transition(State, y) =

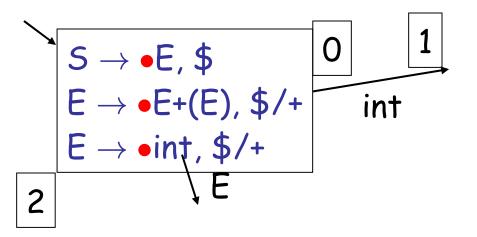
Items \leftarrow \emptyset

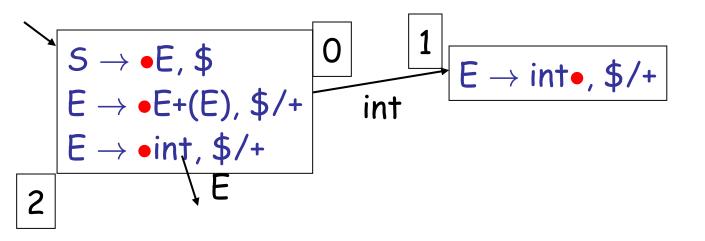
for each [X \rightarrow \alpha \bullet y\beta, b] \in State

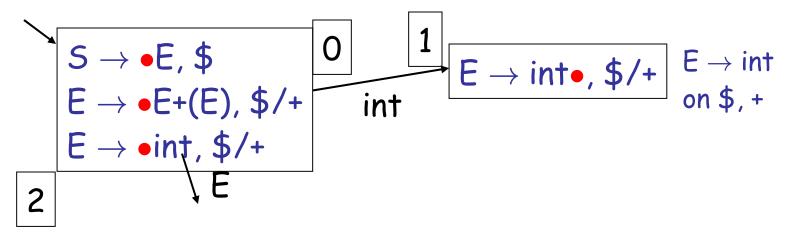
add [X \rightarrow \alpha y \bullet \beta, b] to Items

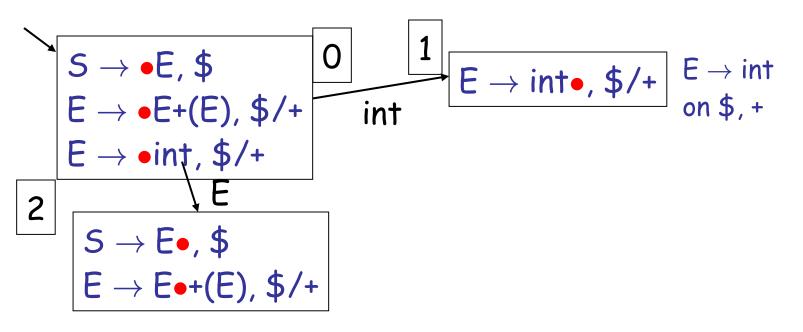
return Closure(Items)
```

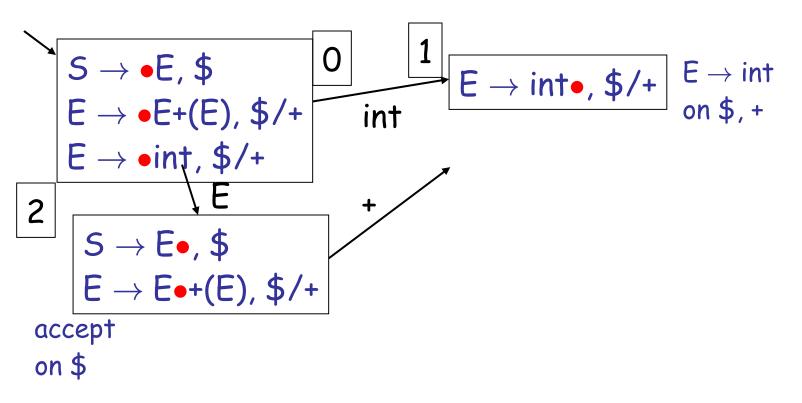


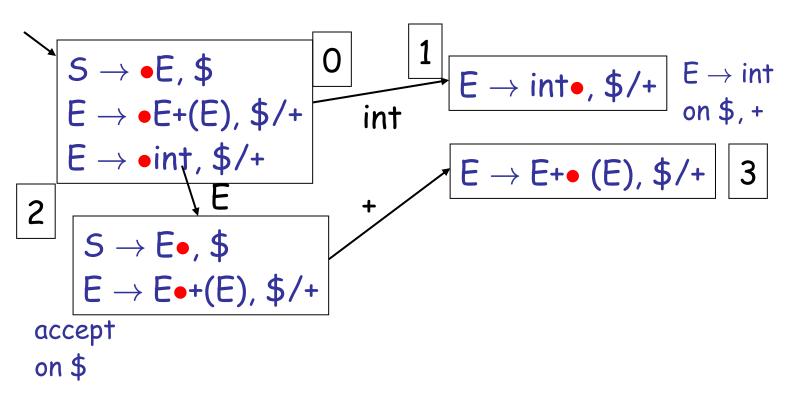


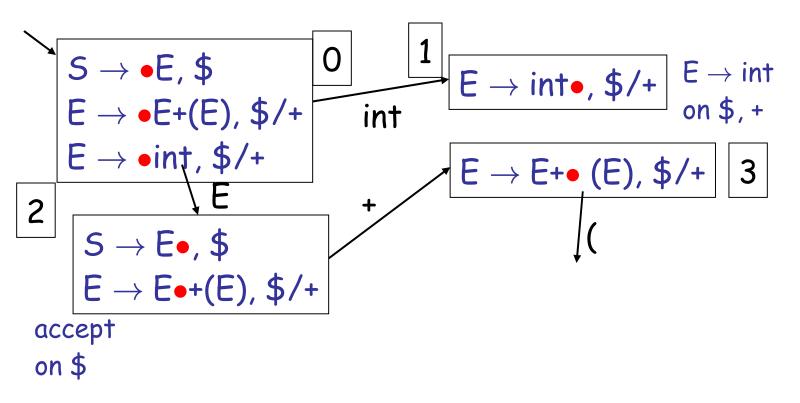


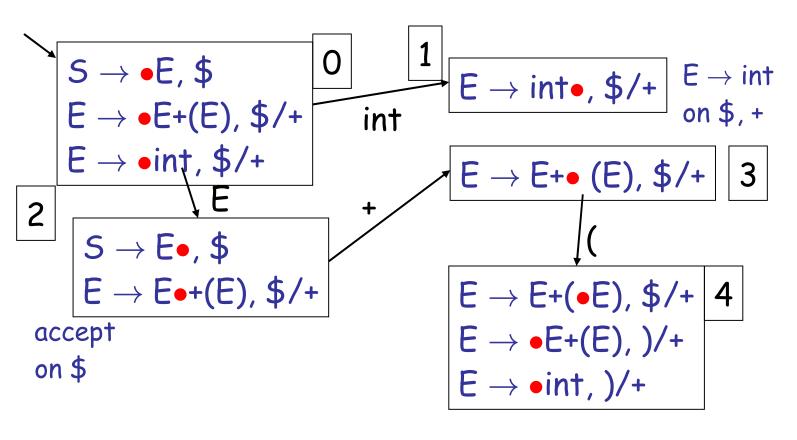


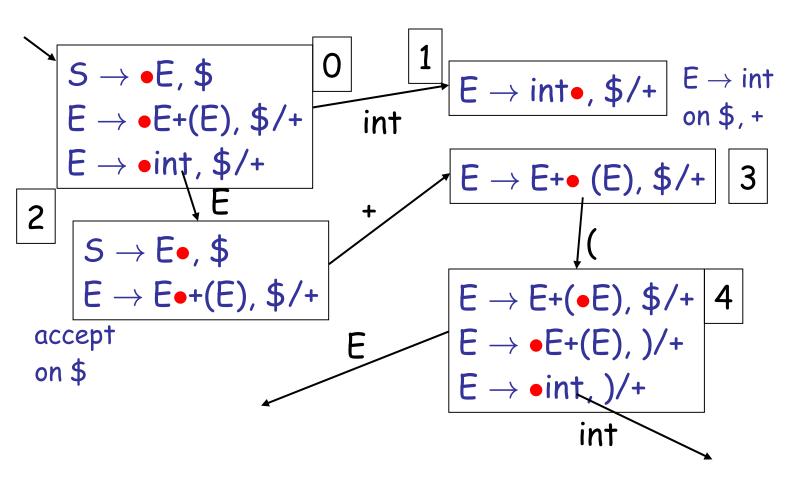


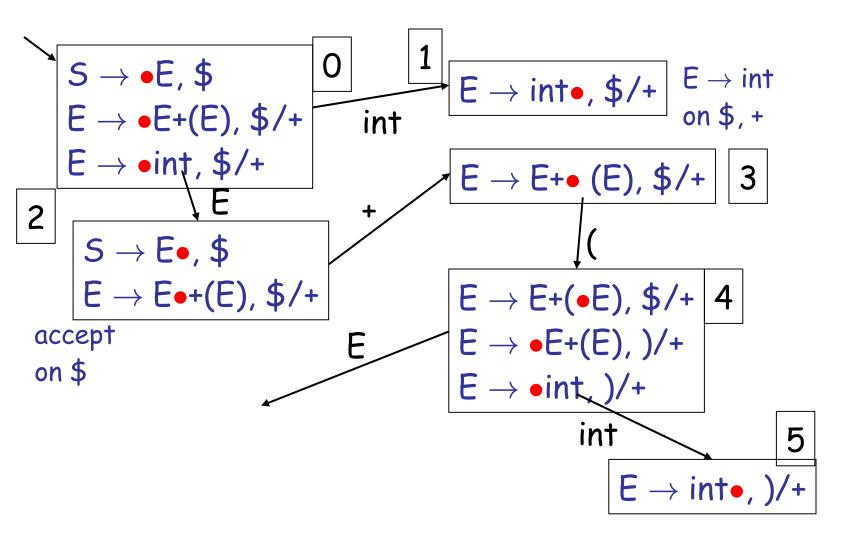


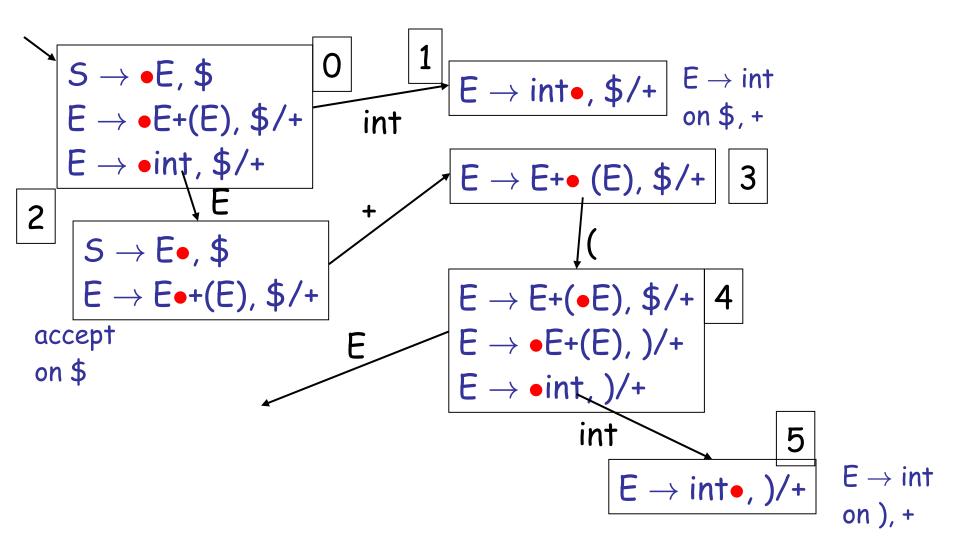


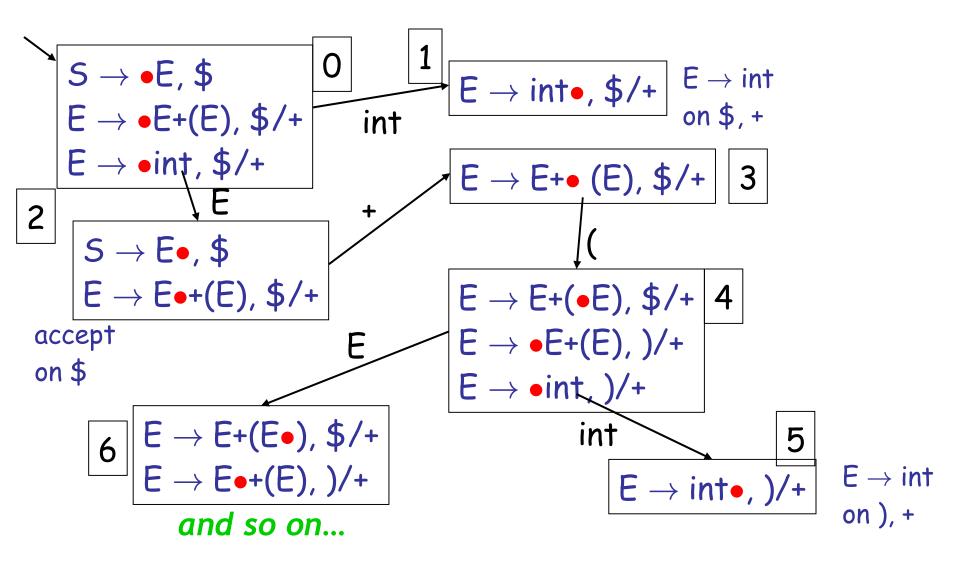












Q: Movies (282 / 842)

 This post-apocalyptic 1984 animated film by Studio Ghibli features a peace-loving, windriding princess who attempts to understand the apparently-evil insects and spreading fungi of her world while averting a war.

Q: Books (722 / 842)

• The 1995 comedy film Clueless starring Alicia Silverstone was based on this Jane Austen novel.

Q: Books (736 / 842)

- Give the last word in 2 of the following 4 young adult book titles:
 - Beverly Cleary Ramona Quimby, Age
 - Judy Blume's Tales of a Fourth
 Grade
 - Lynne Reid Banks's The Indian in the
 - Lloyd Alexander's The High

Q: Games (522 / 842)

• In this 1982 arcade game features lance-wielding knights mounted on giant flying birds and dueling over a pit of lava. Destroying an enemy knight required ramming it such that your lance was higher than the enemy's.

LR Parsing Tables. Notes

- Parsing tables (= the DFA) can be constructed automatically for a CFG
 - "The tables which cannot be constructed are constructed automatically in response to a CFG input. You asked for a miracle, Theo. I give you the L-R-1." Hans Gruber, <u>Die Hard</u>
- But we still need to understand the construction to work with parser generators
 - e.g., they report errors in terms of sets of items
- What kind of errors can we expect?



PARTY CONFLICT

Sometimes, you should back down.

Shift/Reduce Conflicts

If a DFA state contains both

$$[X \rightarrow \alpha \bullet a\beta, b]$$
 and $[Y \rightarrow \gamma \bullet, a]$

- Then on input "a" we could either
 - Shift into state $[X \rightarrow \alpha a \bullet \beta, b]$, or
 - Reduce with $Y \rightarrow \gamma$

This is called a shift-reduce conflict

Shift/Reduce Conflicts

- Typically due to ambiguities in the grammar
- Classic example: the dangling else

```
S \rightarrow \text{if E then S} \mid \text{if E then S else S} \mid \text{OTHER}
```

Will have DFA state containing

```
[S \rightarrow if E then S•, else]
[S \rightarrow if E then S• else S, x]
```

- If else follows then we can shift or reduce
- Default (bison, CUP, etc.) is to shift
 - Default behavior is as needed in this case

More Shift/Reduce Conflicts

Consider the ambiguous grammar

$$E \rightarrow E + E \mid E * E \mid int$$

We will have the states containing

```
[E \rightarrow E * \bullet E, +] \qquad [E \rightarrow E * E \bullet, +]
[E \rightarrow \bullet E + E, +] \Rightarrow^{E} [E \rightarrow E \bullet + E, +]
```

- Again we have a shift/reduce on input +
 - We need to reduce (* binds more tightly than +)
 - Solution: declare the precedence of * and +

More Shift/Reduce Conflicts

In bison declare precedence and associativity:

```
%left +
%left * // high precedence
```

- Precedence of a rule = that of its last terminal
 - See bison manual for ways to override this default
- Resolve shift/reduce conflict with a shift if:
 - no precedence declared for either rule or terminal
 - input terminal has higher precedence than the rule
 - the precedences are the same and right associative

Using Precedence to Solve S/R Conflicts

Back to our example:

```
[E \rightarrow E * \bullet E, +] \qquad [E \rightarrow E * E \bullet, +]
[E \rightarrow \bullet E + E, +] \Rightarrow^{E} [E \rightarrow E \bullet + E, +]
...
```

 Will choose reduce on input + because precedence of rule E → E * E is higher than of terminal +

Using Precedence to Solve S/R Conflicts

Same grammar as before

$$E \rightarrow E + E \mid E * E \mid int$$

We will also have the states

```
[E \rightarrow E + \bullet E, +] \qquad [E \rightarrow E + E \bullet, +]
[E \rightarrow \bullet E + E, +] \Rightarrow^{E} \qquad [E \rightarrow E \bullet + E, +]
...
```

- Now we also have a shift/reduce on input +
 - We choose reduce because E → E + E and + have the same precedence and + is left-associative

Using Precedence to Solve S/R Conflicts

Back to our dangling else example

```
[S \rightarrow if E then S•, else]
[S \rightarrow if E then S• else S, x]
```

- Can eliminate conflict by declaring else with higher precedence than then
 - Or just rely on the default shift action
- But this starts to look like "hacking the parser"
- Avoid overuse of precedence declarations or you'll end with unexpected parse trees
 - The kiss of death ...

Reduce/Reduce Conflicts

If a DFA state contains both

$$[X \rightarrow \alpha \bullet, a]$$
 and $[Y \rightarrow \beta \bullet, a]$

 Then on input "a" we don't know which production to reduce

This is called a reduce/reduce conflict

Reduce/Reduce Conflicts

- Usually due to gross ambiguity in the grammar
- Example: a sequence of identifiers

$$S \rightarrow \varepsilon \mid id \mid id S$$

There are two parse trees for the string id

$$S \rightarrow id$$

 $S \rightarrow id S \rightarrow id$

How does this confuse the parser?

More on Reduce/Reduce Conflicts

Consider the states

Sider the states
$$[S \rightarrow id \bullet, \$]$$

 $[S' \rightarrow \bullet S, \$]$ $[S \rightarrow id \bullet S, \$]$
 $[S \rightarrow \bullet, \$]$ \Rightarrow^{id} $[S \rightarrow \bullet, \$]$
 $[S \rightarrow \bullet id, \$]$ $[S \rightarrow \bullet id, \$]$
 $[S \rightarrow \bullet id S, \$]$ $[S \rightarrow \bullet id S, \$]$

Reduce/reduce conflict on input \$

$$S' \rightarrow S \rightarrow id$$

 $S' \rightarrow S \rightarrow id S \rightarrow id$

• Better rewrite the grammar: $S \rightarrow \varepsilon$ | id S

Can's someone learn this for me?

No, you can't have a neural network



Using Parser Generators

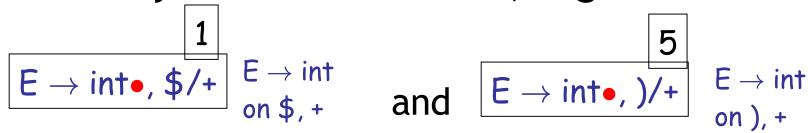
- Parser generators construct the parsing DFA given a CFG
 - Use precedence declarations and default conventions to resolve conflicts
 - The parser algorithm is the same for all grammars (and is provided as a library function)
- But most parser generators do not construct the DFA as described before
 - Why might that be?

Using Parser Generators

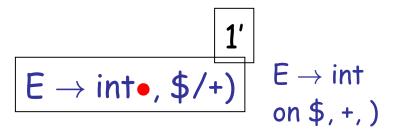
- Parser generators construct the parsing DFA given a CFG
 - Use precedence declarations and default conventions to resolve conflicts
 - The parser algorithm is the same for all grammars (and is provided as a library function)
- But most parser generators do not construct the DFA as described before
 - Because the LR(1) parsing DFA has 1000s of states even for a simple language

LR(1) Parsing Tables are Big

• But many states are similar, e.g.



- Idea: merge the DFA states whose items differ only in the lookahead tokens
 - We say that such states have the same core
- We obtain



The Core of a Set of LR Items

- Definition: The core of a set of LR items is the set of first components
 - Without the lookahead terminals

Example: the core of

{ [X
$$\rightarrow \alpha \bullet \beta$$
, b], [Y $\rightarrow \gamma \bullet \delta$, d]}

is

$$\{X \to \alpha \bullet \beta, Y \to \gamma \bullet \delta\}$$

LALR States

Consider for example the LR(1) states

```
\{[X \rightarrow \alpha \bullet, a], [Y \rightarrow \beta \bullet, c]\}\{[X \rightarrow \alpha \bullet, b], [Y \rightarrow \beta \bullet, d]\}
```

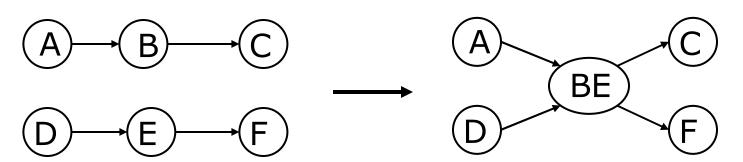
- They have the same core and can be merged
- And the merged state contains:

$$\{[X \rightarrow \alpha \bullet, a/b], [Y \rightarrow \beta \bullet, c/d]\}$$

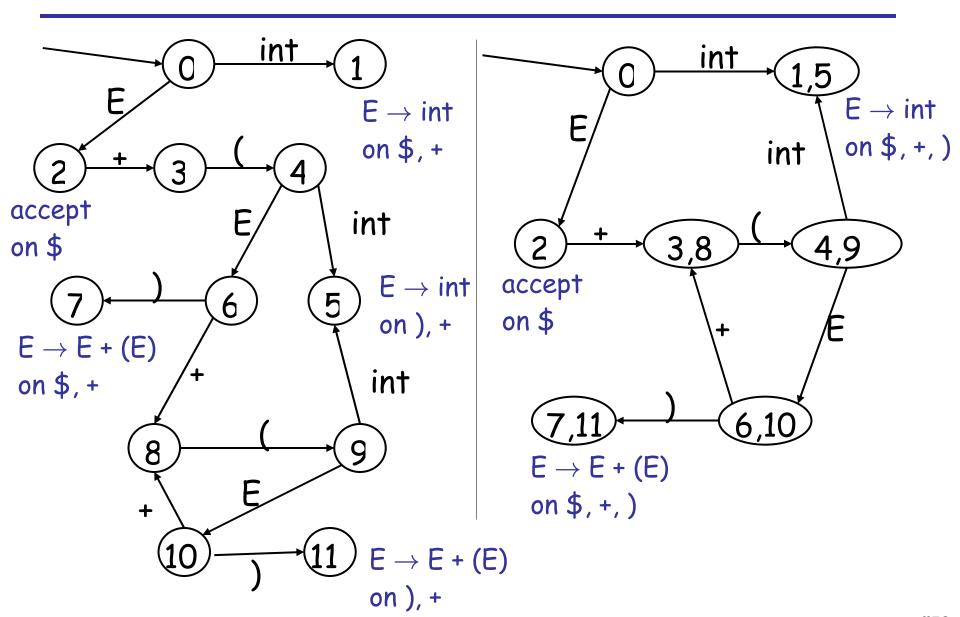
- These are called LALR(1) states
 - Stands for LookAhead LR
 - Typically 10x fewer LALR(1) states than LR(1)

LALR(1) DFA

- Repeat until all states have distinct core
 - Choose two distinct states with same core
 - Merge the states by creating a new one with the union of all the items
 - Point edges from predecessors to new state
 - New state points to all the previous successors



Example LALR(1) to LR(1)



The LALR Parser Can Have Conflicts

• Consider for example the LR(1) states

$$\{[X \rightarrow \alpha \bullet, a], [Y \rightarrow \beta \bullet, b]\}$$
$$\{[X \rightarrow \alpha \bullet, b], [Y \rightarrow \beta \bullet, a]\}$$

And the merged LALR(1) state

$$\{[X \rightarrow \alpha \bullet, a/b], [Y \rightarrow \beta \bullet, a/b]\}$$

Has a new reduce-reduce conflict

In practice such cases are rare

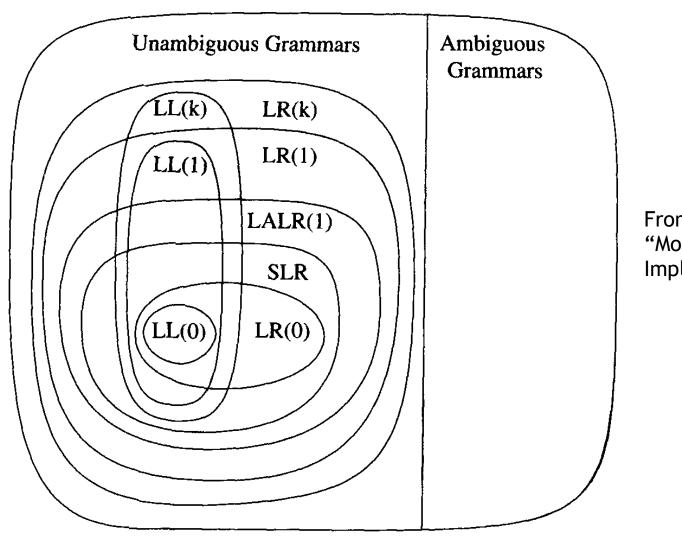
LALR vs. LR Parsing

- LALR languages are not natural
 - They are an efficiency hack on LR languages

- Any "reasonable" programming language has a LALR(1) grammar
 - Java and C++ are presumed unreasonable ...

 LALR(1) has become a standard for programming languages and for parser generators

A Hierarchy of Grammar Classes

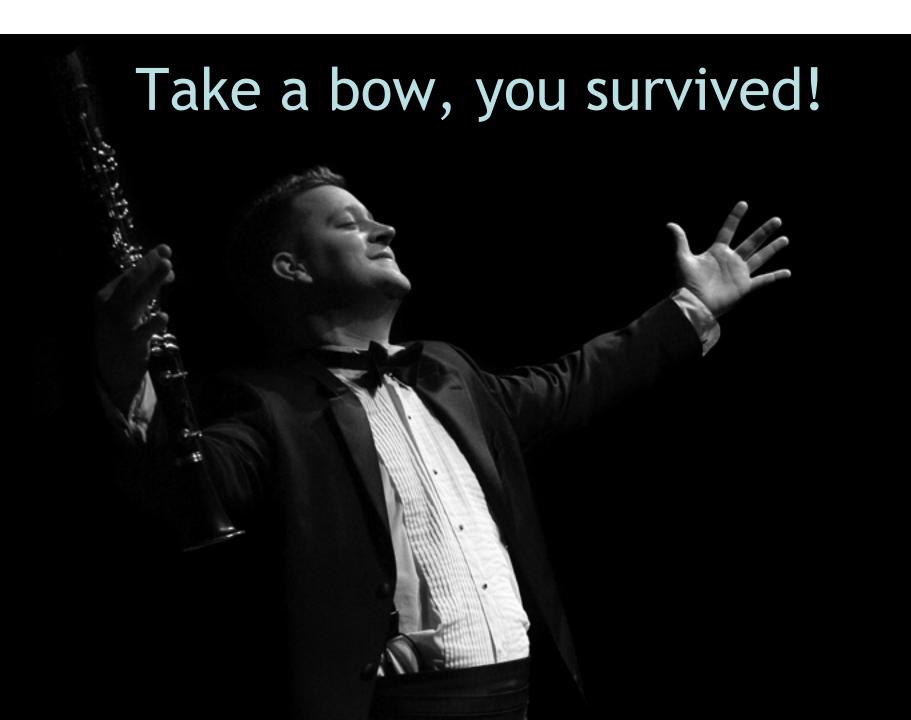


From Andrew Appel, "Modern Compiler Implementation in Java"

Notes on Parsing

- Parsing
 - A solid foundation: context-free grammars
 - A simple parser: LL(1)
 - A more powerful parser: LR(1)
 - An efficiency hack: LALR(1)
 - LALR(1) parser generators

Now we move on to semantic analysis



Supplement to LR Parsing

Strange Reduce/Reduce Conflicts
Due to LALR Conversion
(from the bison manual)

Strange Reduce/Reduce Conflicts

Consider the grammar

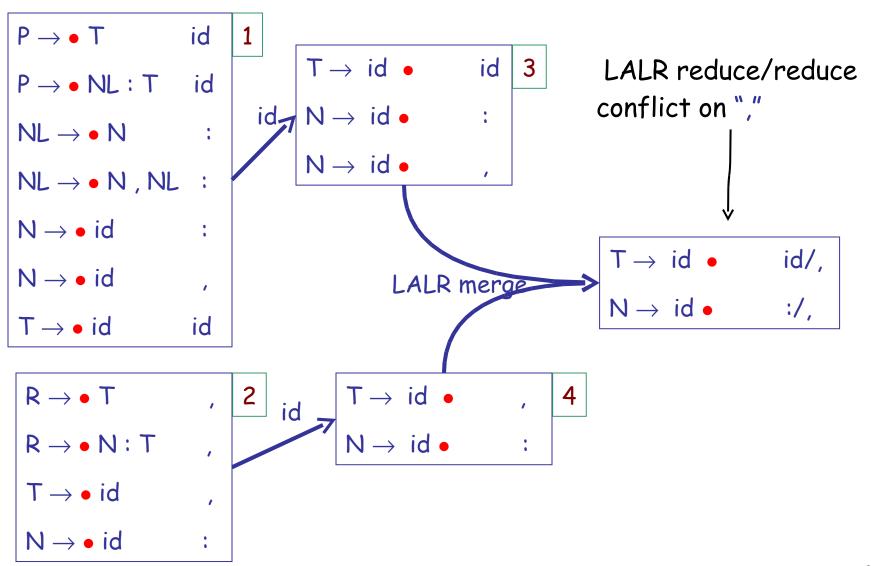
```
S 	o PR, NL 	o N \mid N, NL P 	o T \mid NL:T R 	o T \mid N:T N 	o id T 	o id
```

- P parameters specification
- R result specification
- N a parameter or result name
- T a type name
- NL a list of names

Strange Reduce/Reduce Conflicts

- In P an id is a
 - N when followed by, or:
 - T when followed by id
- In R an id is a
 - N when followed by:
 - T when followed by,
- This is an LR(1) grammar.
- But it is not LALR(1). Why?
 - For obscure reasons

A Few LR(1) States



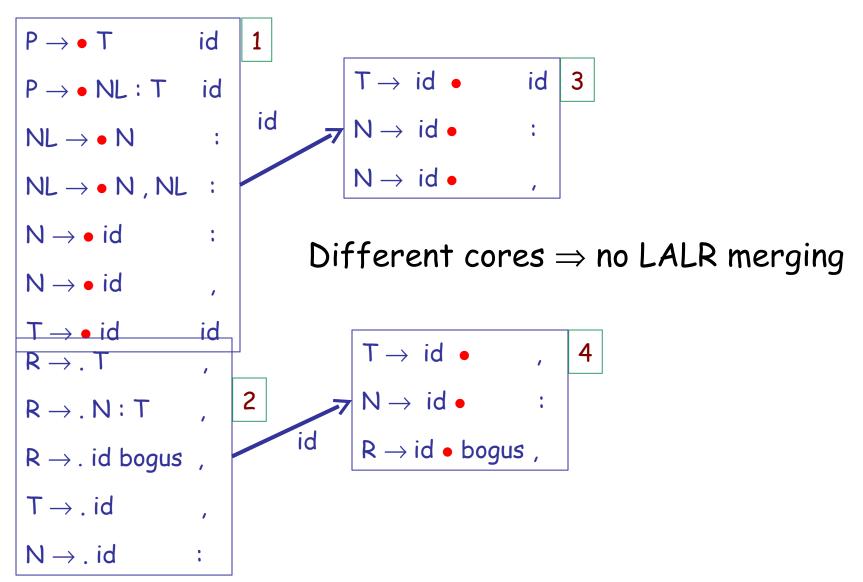
What Happened?

- Two distinct states were confused because they have the same core
- Fix: add dummy productions to distinguish the two confused states
- E.g., add

$R \rightarrow id bogus$

- bogus is a terminal not used by the lexer
- This production will never be used during parsing
- But it distinguishes R from P

A Few LR(1) States After Fix



Homework

- Today: WA2 Was Due
- Thursday: Chapter 3.1 3.6
 - Optional Wikipedia Article
- Tuesday Sep 29 Midterm 1 in Class
- Wednesday: PA3 due
 - Parsing!
- Thursday: WA3 due