Parking For **Drive-Thru** Service MoreOnly **Static** Semantics **Thank You**

Midterm 1 Results

- Score range 63.5 to 102, average 88.75
 - I am quite pleased.
- Answer Key available on Web
- Toughest Problems:
 - LL Parsing
 - LR Parsing

Midterm 1 Suggestions

- class time @ 5pm; the time it is scheduled
- sometimes pace is fast like for Fold
- time commitment but I'm taking 5 credits
 - the workload; disproportionate amount of work compared to other classes (but you warned us :-))
 - length of PAs; staying up late to finish PAs
- theory and greek letters x2
- not getting candy; getting mints FML
- being underground
- coding in C; semicolons in Cool; Ocaml error reporting; Ocaml
- midterm; the tests
- can't think of anything
- material that is "implied prerequisities"
- slide examples are verbose and hard to follow
- "vaguely-specified" PAs
- cold-calling



One-Slide Summary

- Typing rules formalize the semantics checks necessary to validate a program. Well-typed programs do not go wrong.
- Subtyping relations (≤) and least-upper-bounds (lub) are powerful tools for type-checking dynamic dispatch.
- We will use SELF_TYPE_c for "C or any subtype of C". It will show off the subtlety of type systems and allow us to check methods that return self objects.

Lecture Outline

- Typing Rules
- Dispatch Rules
 - Static
 - Dynamic
- SELF_TYPE

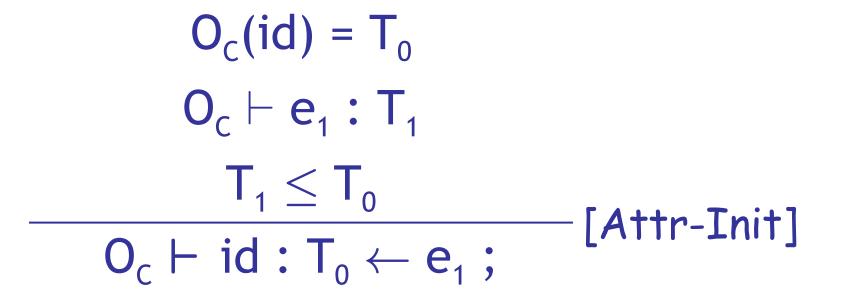
Assignment

What is this thing? What's \vdash ? **O**? \leq ?

 $O(id) = T_0$ $O \vdash e_1 : T_1$ $T_1 \leq T_0$ $O \vdash id \leftarrow e_1 : T_1$ [Assign]

Initialized Attributes

- Let O_c(x) = T for all attributes x:T in class C
 - O_c represents the class-wide scope
 - we "preload" the environment O with all attributes
- Attribute initialization is similar to let, except for the scope of names



If-Then-Else

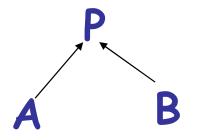
- Consider: if e_0 then e_1 else e_2 fi
- The result can be either e_1 or e_2
- The dynamic type is either e_1 's or e_2 's type
- The best we can do statically is the smallest supertype larger than the type of e_1 and e_2



Watch NEWS 25 for weather changes throughout the day

If-Then-Else example

• Consider the class hierarchy



• ... and the expression

if ... then new A else new B fi

- Its type should allow for the dynamic type to be both A or B
 - Smallest supertype is P

Least Upper Bounds

- Define: lub(X,Y) to be the least upper bound of X and Y. lub(X,Y) is Z if
 - $X \le Z \land Y \le Z$

Z is an upper bound

- $X \leq Z' \land Y \leq Z' \Rightarrow Z \leq Z'$

Z is least among upper bounds

 In Cool, the least upper bound of two types is their least common ancestor in the inheritance tree

If-Then-Else Revisited

 $O \vdash e_0 : Bool$ $O \vdash e_1 : T_1$ $O \vdash e_2 : T_2$

 $O \vdash if e_0 then e_1 else e_2 fi : lub(T_1, T_2)$

[If-Then-Else]

 The rule for case expressions takes a lub over all branches

 $O \vdash e_0 : T_0$ $O[T_1/x_1] \vdash e_1 : T_1'$

 $O[T_n/x_n] \vdash e_n : T_n'$

 $O \vdash case e_0 \text{ of } x_1:T_1 \Rightarrow e_1;$...; $x_n : T_n \Rightarrow e_n; esac : lub(T_1',...,T_n')$

Method Dispatch

• There is a problem with type checking method calls:

 $O \vdash e_0 : T_0$ $O \vdash e_1 : T_1$ \cdots $O \vdash e_n : T_n$ $O \vdash e_0.f(e_1, \dots, e_n) : ?$ $O \vdash e_0.f(e_1, \dots, e_n) : ?$

 We need information about the formal parameters and return type of f

Notes on Dispatch

- In Cool, method and object identifiers live in different name spaces
 - A method foo and an object foo can coexist in the same scope
- In the type rules, this is reflected by a separate mapping M for method signatures: M(C,f) = (T₁,...,T_n,T_{n+1}) means in class C there is a method f f(x₁:T₁,...,x_n:T_n): T_{n+1}

An Extended Typing Judgment

- Now we have *two* environments: O and M
- The form of the typing judgment is O, $M \vdash e : T$

read as: "with the assumption that the object identifiers have types as given by O and the method identifiers have signatures as given by M, the expression e has type T"

The Method Environment

- The method environment must be added to all rules
- In most cases, M is passed down but not actually used
 - Example of a rule that does not use M:

$$0, M \vdash e_1 : T_1$$
$$0, M \vdash e_2 : T_2$$
$$[Add]$$
$$0, M \vdash e_1 + e_2 : Int$$

- Only the dispatch rules uses M

The Dispatch Rule Revisited

Check receiver
object e₀ **O**, $\mathbf{M} \vdash \mathbf{e}_{0} : \mathbf{T}_{0}$ O, $M \vdash e_1 : T_1$ Check actual arguments $O, M \vdash e_n : T_n$ \Box Look up formal argument types T_i ? $M(T_{0}, f) = (T_{1}', ..., T_{n}', T_{n+1}')$ $T_i \leq T_i$ (for $1 \leq i \leq n$) [Dispatch] $O, M \vdash e_0.f(e_1,...,e_n) : T_{n+1}'$

Static Dispatch

- Static dispatch is a variation on normal dispatch
- The method is found in the class explicitly named by the programmer (not via e₀)

• The inferred type of the dispatch expression must conform to the specified type

Static Dispatch (Cont.)

$$O, M \vdash e_{0} : T_{0}$$

$$O, M \vdash e_{1} : T_{1}$$

$$...$$

$$O, M \vdash e_{n} : T_{n}$$

$$T_{0} \leq T$$

$$M(T, f) = (T_{1}', ..., T_{n}', T_{n+1}')$$

$$T_{i} \leq T_{i}' \quad (for \ 1 \leq i \leq n)$$

$$O, M \vdash e_{0} \otimes T.f(e_{1}, ..., e_{n}) : T_{n+1}'$$
[StaticDispatch]

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How should we handle SELF_TYPE ?

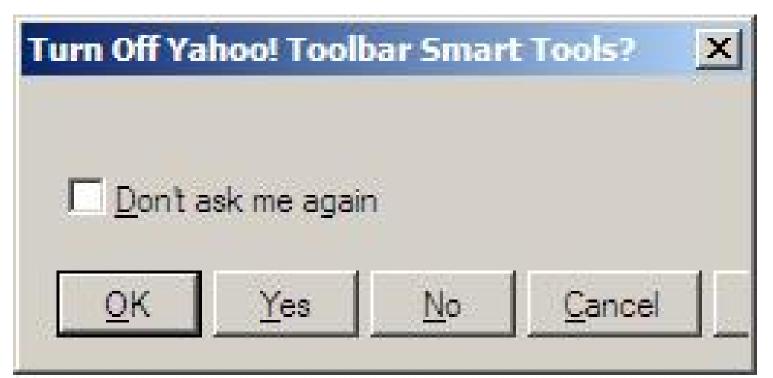


Flexibility vs. Soundness

- Recall that type systems have two conflicting goals:
 - Give flexibility to the programmer
 - Prevent valid programs from "going wrong"
 - Milner, 1981: "Well-typed programs do not go wrong"
- An active line of research is in the area of inventing more flexible type systems while preserving soundness

Dynamic And Static Types

- The dynamic type of an object is ?
- The static type of an expression is ?
- You tell me!



Dynamic And Static Types

- The dynamic type of an object is the class C that is used in the "new C" expression that created it
 - A run-time notion
 - Even languages that are not statically typed have the notion of dynamic type
- The static type of an expression is a notation that captures all possible dynamic types the expression could take
 - A compile-time notion

Soundness

Soundness theorem for the Cool type system:

 \forall E. dynamic_type(E) \leq static_type(E)

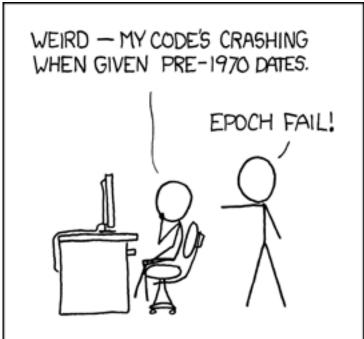
Why is this OK?

- All operations that can be used on an object of type C can also be used on an object of type C' \leq C
 - Such as fetching the value of an attribute
 - Or invoking a method on the object
- Subclasses can only add attributes or methods
- Methods can be redefined but with same type!

An Example

```
class Count {
   i : int \leftarrow 0;
   inc () : Count {
           i \leftarrow i + 1;
           self;
              But there is disaster lurking in
              the type system!
   };
};
```

- Class Count incorporates a counter
- The inc method works for any subclass



Continuing Example

Consider a subclass Stock of Count

class Stock inherits Count {
 name() : String { ...}; -- name of item
};

• And the following use of **Stock**:

```
class Main {
    a : Stock ← (new Stock).inc ();
    a.name() ...
};
Type checking
error !
```

Post-Mortem

- (new Stock).inc() has dynamic type Stock
- So it is legitimate to write

a : Stock ← (new Stock).inc ()

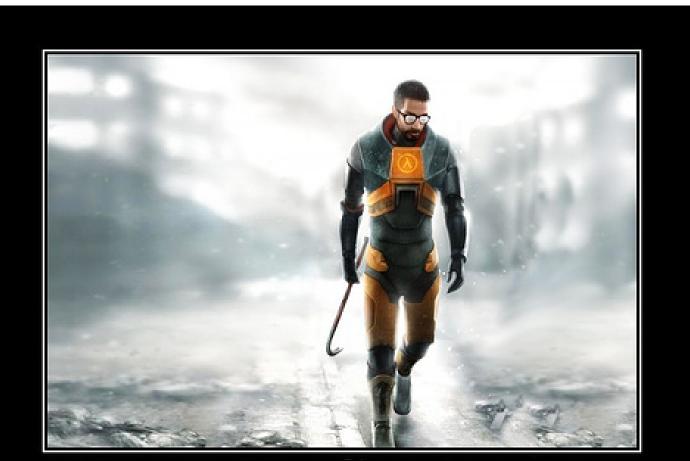
But this is not well-typed

(new Stock).inc() has static type Count

- The type checker "loses" type information
- This makes inheriting inc useless
 - So, we must redefine inc for each of the subclasses, with a specialized return type



I Need A Hero!



Type Systems

One tool. One million uses.

SELF_TYPE to the Rescue

- We will extend the type system
- Insight:
 - inc returns "self"
 - Therefore the return value has same type as "self"
 - Which could be Count or any subtype of Count!
 - In the case of (new Stock).inc() the type is Stock
- We introduce the keyword SELF_TYPE to use for the return value of such functions
 - We will also modify the typing rules to handle SELF_TYPE

SELF_TYPE to the Rescue (2)

- SELF_TYPE allows the return type of inc to change when inc is inherited
- Modify the declaration of inc to read

inc() : SELF_TYPE { ... }

• The type checker can now prove:

0, M ⊢ (new Count).inc() : Count
0, M ⊢ (new Stock).inc() : Stock

• The program from before is now well typed

SELF_TYPE: Binford Tools



- SELF_TYPE is not a dynamic type
- SELF_TYPE is a static type
- It helps the type checker to keep better track of types
- It enables the type checker to accept more correct programs
- In short, having SELF_TYPE increases the expressive power of the type system

SELF_TYPE and Dynamic Types (Example)

- What can be the dynamic type of the object returned by inc?
 - Answer: whatever could be the type of "self"

class A inherits Count { }; class B inherits Count { }; class C inherits Count { }; (inc could be invoked through any of these classes)

- Answer: Count or any subtype of Count

SELF_TYPE and Dynamic Types (Example)

 In general, if SELF_TYPE appears textually in the class C as the declared type of E then it denotes the dynamic type of the "self" expression:

dynamic_type(E) = dynamic_type(self) \leq C

- Note: The meaning of SELF_TYPE depends on where it appears
 - We write SELF_TYPE_c to refer to an occurrence of SELF_TYPE in the body of C

Type Checking

- This suggests a typing rule: $SELF_TYPE_c \leq C$
- This rule has an important consequence:
 - In type checking it is always safe to replace SELF_TYPE_c by C
- This suggests one way to handle SELF_TYPE :
 Replace all occurrences of SELF_TYPE_c by C
- This would be correct but it is like not having SELF_TYPE at all (whoops!)

Operations on SELF_TYPE

- Recall the operations on types
 - $T_1 \leq T_2$ T_1 is a subtype of T_2
 - $lub(T_1,T_2)$ the least-upper bound of T_1 and T_2
- We must extend these operations to handle SELF_TYPE
- Might take some time ...



Q: Games (503 / 842)

 This 1983 adventure game designed by Roberta Williams described Sir Graham's attempts to recover the three magical treasures of Daventry and become the next king. It featured a parser for simple textual commands (e.g., "get carrot") and spawned numerous sequels.

Q: Movies (316 / 842)

 Name the star and the 1990 holiday film that features Joe Pesci and Daniel Stern as the "Wet Bandits" and a child, too young to shave, who defends a house.

Q: Books (745 / 842)

 Name the 1965 Frank Herbert scinovel that features sandworms, the house Harkonnen, and the quote "What's in the box? / Pain." It won the Hugo and Nebula awards and usually considered the best-selling sci-fi novel of all time.

Q: Movies (292 / 842)

 From the 1981 movie Raiders of the Lost Ark, give either the protagonist's phobia or composer of the musical score.

Extending \leq

Let T and T' be any types except SELF_TYPE There are four cases in the definition of \leq

- SELF_TYPE_c \leq T if C \leq T
 - SELF_TYPE_c can be any subtype of C
 - This includes C itself
 - Thus this is the most flexible rule we can allow
- SELF_TYPE_c \leq SELF_TYPE_c
 - SELF_TYPE_c is the type of the "self" expression
 - In Cool we never need to compare SELF_TYPEs coming from different classes

Extending \leq (Cont.)

- T ≤ SELF_TYPE_c always false
 Note: SELF_TYPE_c can denote any subtype of C.
- $T \leq T'$ (according to the rules from before)

Based on these rules we can extend lub ...

Extending lub(T,T')

- Let T and T' be any types except SELF_TYPE Again there are four cases:
- lub(SELF_TYPE_c, SELF_TYPE_c) = SELF_TYPE_c
- $lub(SELF_TYPE_c, T) = lub(C, T)$ This is the best we can do because $SELF_TYPE_c \le C$
- lub(T, SELF_TYPE_c) = lub(C, T)
- lub(T, T') defined as before

Where Can SELF_TYPE Appear in COOL?

- The parser checks that SELF_TYPE appears only where a type is expected
- But SELF_TYPE is not allowed everywhere a type can appear:
- class T inherits T' {...}
 - T, T' cannot be SELF_TYPE
 - Because SELF_TYPE is never a dynamic type
- x : T
 - T can be SELF_TYPE
 - An attribute whose type is SELF_TYPE_c

Where Can SELF_TYPE Appear in COOL?

- 1. let x : T in E
 - T can be SELF_TYPE
 - x has type SELF_TYPE_c
- 2. new T
 - T can be SELF_TYPE
 - Creates an object of the same type as self
- m@T($E_1,...,E_n$)
 - T cannot be SELF_TYPE

Typing Rules for SELF_TYPE

- Since occurrences of SELF_TYPE depend on the enclosing class we need to carry more context during type checking
- New form of the typing judgment:

O,M,C ⊢ e : **T**

(An expression e occurring in the body of C has static type T given a variable type environment O and method signatures M)

Type Checking Rules

- The next step is to design type rules using SELF_TYPE for each language construct
- Most of the rules remain the same except that < and lub are the new ones
- Example:

 $O(id) = T_0$ $O,M,C \vdash e_1 : T_1$ $T_1 \leq T_0$

 $O,M,C \vdash id \leftarrow e_1 : T_1$

What's Different?

• Recall the old rule for dispatch $O,M,C \vdash e_0 : T_0$

```
\begin{array}{l}
        ... \\
        O,M,C \vdash e_{n}: T_{n} \\
        M(T_{0'},f) = (T_{1'},...,T_{n'},T_{n+1'}) \\
        T_{n+1}' \neq SELF\_TYPE \\
        T_{i} \leq T_{i}' \qquad 1 \leq i \leq n \\
        O,M,C \vdash e_{0}.f(e_{1'}...,e_{n}): T_{n+1}'
\end{array}
```

The Big Rule for SELF_TYPE

• If the return type of the method is SELF_TYPE then the type of the dispatch is the type of the dispatch expression:

 $O,M,C \vdash e_o : T_o$

 $\begin{array}{l}
\textbf{O}, \textbf{M}, \textbf{C} \vdash \textbf{e}_{n} : \textbf{T}_{n} \\
\textbf{M}(\textbf{T}_{0'}, \textbf{f}) = (\textbf{T}_{1}', \dots, \textbf{T}_{n}', \textbf{SELF}_{\textbf{TYPE}}) \\
\textbf{T}_{i} \leq \textbf{T}_{i}' \qquad \textbf{1} \leq i \leq n \\
\textbf{O}, \textbf{M}, \textbf{C} \vdash \textbf{e}_{0} \cdot \textbf{f}(\textbf{e}_{1}, \dots, \textbf{e}_{n}) : \textbf{T}_{0}
\end{array}$

What's Different?

- Note this rule handles the **Stock** example
- Formal parameters cannot be SELF_TYPE
- Actual arguments can be SELF_TYPE
 The extended < relation handles this case
- The type T₀ of the dispatch expression could be SELF_TYPE
 - Which class is used to find the declaration of f?
 - Answer: it is safe to use the class where the dispatch appears

Static Dispatch

• Recall the original rule for static dispatch

O,M,C ⊢ **e**₀ : **T**₀

O,M,C ⊢ **e**_n : **T**_n $T_n \leq T$ $M(T, f) = (T_1', ..., T_n', T_{n+1}')$ $T_{n+1}' \neq SELF_TYPE$ $T_i \leq T_i'$ $1 \leq i \leq n$ $O,M,C \vdash e_0 @T.f(e_1,...,e_n) : T_{n+1}'$

Static Dispatch

• If the return type of the method is SELF_TYPE we have:

```
O,M,C \vdash e_0 : T_0
             O,M,C ⊢ e<sub>n</sub> : T<sub>n</sub>
                    T_0 \leq T
M(T, f) = (T_{1}', ..., T_{n}', SELF_TYPE)
        T_i \leq T_i' 1 \leq i \leq n
   O,M,C \vdash e_0 @T.f(e_1,...,e_n) : T_0
```

Static Dispatch

- Why is this rule correct?
- If we dispatch a method returning SELF_TYPE in class T, don't we get back a T?
- No. SELF_TYPE is the type of the self parameter, which may be a subtype of the class in which the method body appears
 - Not the class in which the call appears!
- The static dispatch class cannot be **SELF_TYPE**

New Rules

• There are two new rules using **SELF_TYPE**

O,M,C ⊢ self : SELF_TYPE_c

O,M,C ⊢ new **SELF_TYPE** : **SELF_TYPE**_c

• There are a number of other places where SELF_TYPE is used

Where is SELF_TYPE Illegal in COOL?

- m(x : T) : T' { ... }
 - Only T' can be SELF_TYPE !

What could go wrong if T were SELF_TYPE?

class A { comp(x : SELF_TYPE) : Bool {...}; }; class B inherits A { b() : int { ... }; comp(y : SELF_TYPE) : Bool { ... y.b() ...}; };

....

let x : A ← new B in ... x.comp(new A); ...

Summary of SELF_TYPE

- The extended < and lub operations can do a lot of the work. Implement them to handle SELF_TYPE
- SELF_TYPE can be used only in a few places. Be sure it isn't used anywhere else.
- A use of SELF_TYPE always refers to any subtype in the current class
 - The exception is the type checking of dispatch.
 - SELF_TYPE as the return type in an invoked method might have nothing to do with the current class

Why Cover SELF_TYPE ?

- SELF_TYPE is a research idea
 - It adds more expressiveness to the type system
- SELF_TYPE is itself not so important
 - except for the project
- Rather, SELF_TYPE is meant to illustrate that type checking can be quite subtle
- In practice, there should be a balance between the complexity of the type system and its expressiveness

Type Systems

- The rules in these lecture were Cool-specific
 - Other languages have very different rules
 - We'll survey a few more type systems later
- General themes
 - Type rules are defined on the structure of expressions
 - Types of variables are modeled by an environment
- Types are a play between flexibility and safety

Homework

- No WA due this week
- No PA due this week
- PA4/WA4 Checkpoint Due Wed Oct 14
- For Next Time: Read Chapters 8.1-8.3
 - Optional Grant & Smith