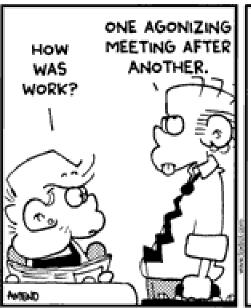
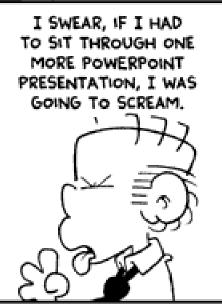
Lexical Analysis

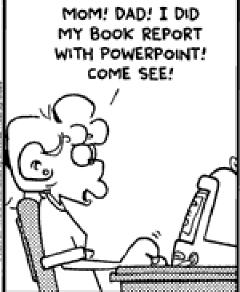
Finite Automata

(Part 2 of 2)



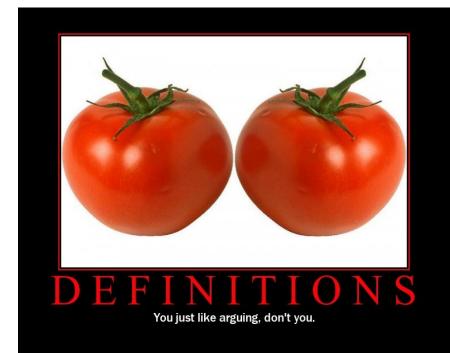






PA1, PA1c

 You can submit new rosetta.yada files for PA1, so you can fix errors from PA1c.





Reading Quiz Results

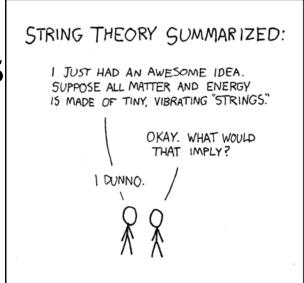
- Average: 2.11 / 4.00 = 53%
- Standard Dev: 1.00
- Goal was 85%
- Particularly troubling was that two-thirds of the class missed "Speedcoding" ...
 - ... which was the *name* of the assigned reading. You didn't even have to *read* the paper to get it, you just had to *look* at the assignment list.
- This gives me **no** confidence that the majority of students are reading for comprehension.

Cunning Plan

Regular expressions provide a concise

notation for string patterns

- Use in lexical analysis requires extensions
 - To resolve ambiguities
 - To handle errors
- Good algorithms known (next)
 - Require only single pass over the input
 - Few operations per character (table lookup)



One-Slide Summary

- Finite automata are formal models of computation that can accept regular languages corresponding to regular expressions.
- Nondeterministic finite automata (NFA)
 feature epsilon transitions and multiple
 outgoing edges for the same input symbol.
- Regular expressions can be converted to NFAs.
- Tools will **generate** DFA-based lexer code for you from regular expressions.

Finite Automata

- Regular expressions = specification
- Finite automata = implementation

- A finite automaton consists of
 - An input alphabet Σ
 - A set of states \$
 - A start state n
 - A set of accepting states F ⊆ S
 - A set of transitions state → input state

Finite Automata

Transition

$$S_1 \rightarrow^a S_2$$

Is read

In state s₁ on input "a" go to state s₂

- If end of input (or no transition possible)
 - If in accepting state ⇒ accept
 - Otherwise \Rightarrow reject

Finite Automata State Graphs

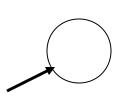
A state

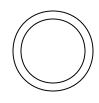


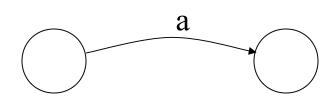
An accepting state

A transition



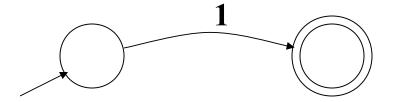






A Simple Example

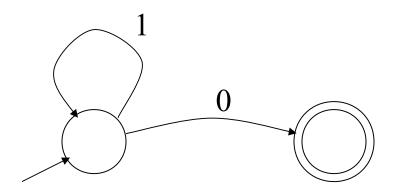
A finite automaton that accepts only "1"



 A finite automaton <u>accepts</u> a string if we can follow transitions labeled with the characters in the string from the start to some accepting state

Another Simple Example

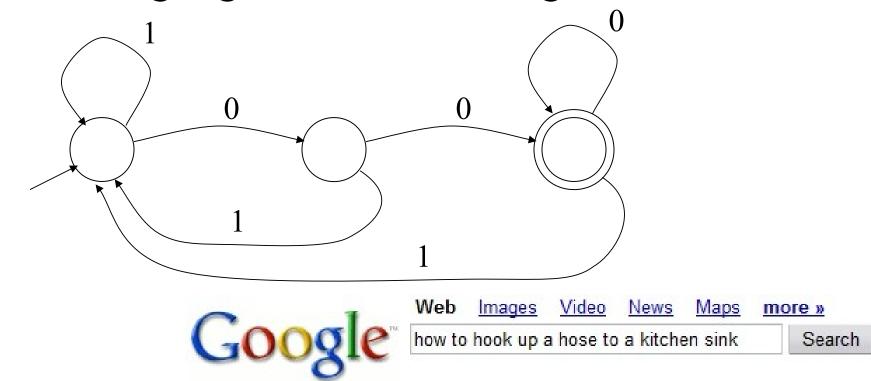
- A finite automaton accepting any number of 1's followed by a single 0
- Alphabet $\Sigma = \{0,1\}$



Check that "1110" is accepted but "110..."
 is not

And Another Example

- Alphabet $\Sigma = \{0,1\}$
- What language does this recognize?

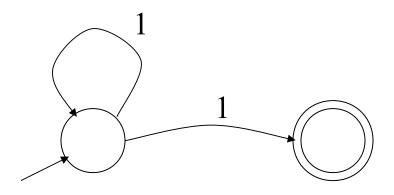


Web

Did you mean: how to hook up a horse to a kitchen sink

And A Fourth Example

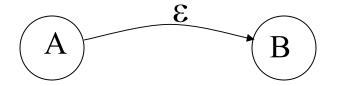
• Alphabet still $\Sigma = \{0, 1\}$



- The operation of the automaton is not completely defined by the input
 - On input "11" the automaton could be in either state

Epsilon Moves

• Another kind of transition: ε-moves



Machine can move from state A to state B

without reading input



Deterministic and Nondeterministic Automata

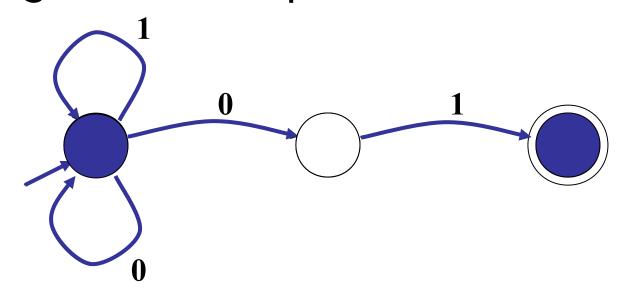
- Deterministic Finite Automata (DFA)
 - One transition per input per state
 - No ε-moves
- Nondeterministic Finite Automata (NFA)
 - Can have multiple transitions for one input in a given state
 - Can have ε-moves
- Finite automata have finite memory
 - Need only to encode the current state

Execution of Finite Automata

- A DFA can take only one path through the state graph
 - Completely determined by input
- NFAs can choose
 - Whether to make ε-moves
 - Which of multiple transitions for a single input to take

Acceptance of NFAs

An NFA can get into multiple states



- Input: 1 0 1
- Rule: NFA accepts if it <u>can</u> get in a final state

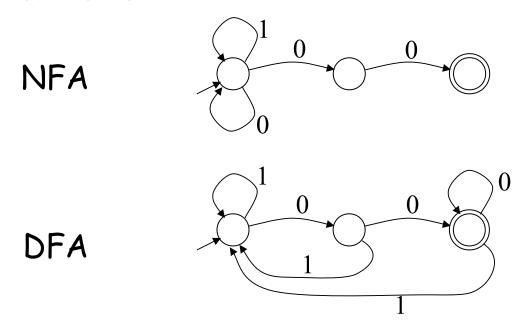
NFA vs. DFA (1)

- NFAs and DFAs recognize the same set of languages (regular languages)
 - They have the same expressive power
- DFAs are easier to implement
 - There are no choices to consider



NFA vs. DFA (2)

 For a given language the NFA can be simpler than the DFA



DFA can be exponentially larger than NFA

Natural Languages

 This North Germanic language is generally mutually intelligible with Norwegian and Danish, and descends from Old Norse of the Viking Era to a modern speaking population of about 10 million people. The language contains two genders, nouns that are rarely inflected, and a typical subject-verb-object ordering. Its home country is one of the largest music exporters of the modern world, often targeting English-speaking audiences. Bands such as Ace of Base, ABBA and Roxette are examples, with over 420m combined album sales.

Unnatural Languages

 This stack-based structured computer programming language appeared in the 1970's and went on to influence PostScript and RPL. It is typeless and is often used in bootloaders and embedded applications. Example:

```
25 10 * 50 +
```

• Simple C Program:

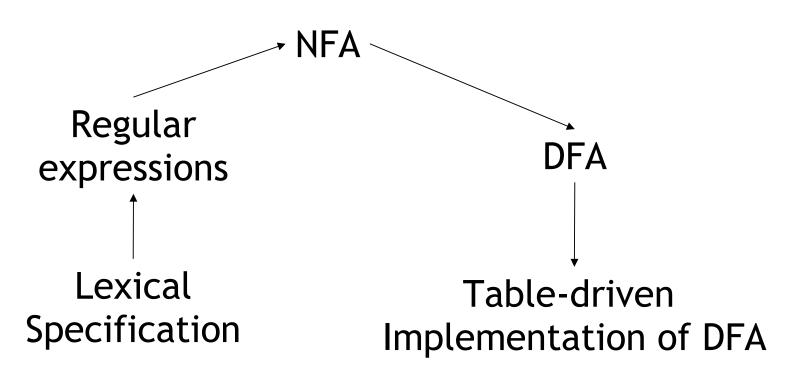
```
int floor5(int v) { return (v < 6) ? 5 : (v - 1); }
```

• Same program in *this* Language:

```
: FLOOR5 ( n -- n' ) DUP 6 < IF DROP 5 ELSE 1 - THEN;
```

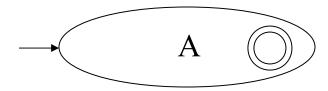
Regular Expressions to Finite Automata

High-level sketch

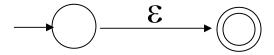


Regular Expressions to NFA (1)

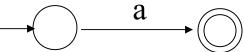
- For each kind of rexp, define an NFA
 - Notation: NFA for rexp A



• For ε

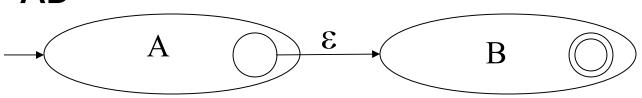


For input a

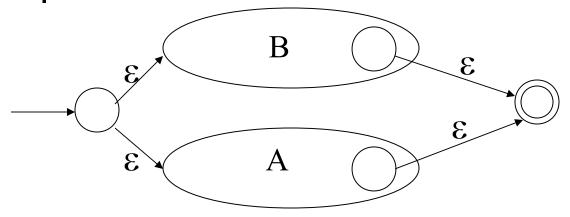


Regular Expressions to NFA (2)

For AB

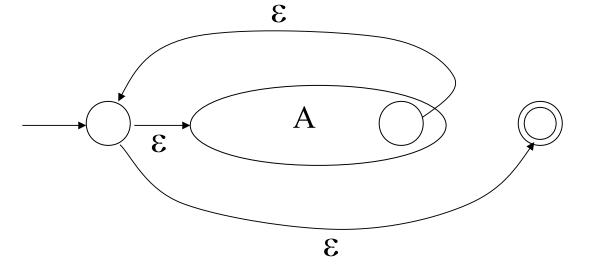


• For A | B



Regular Expressions to NFA (3)

For A*









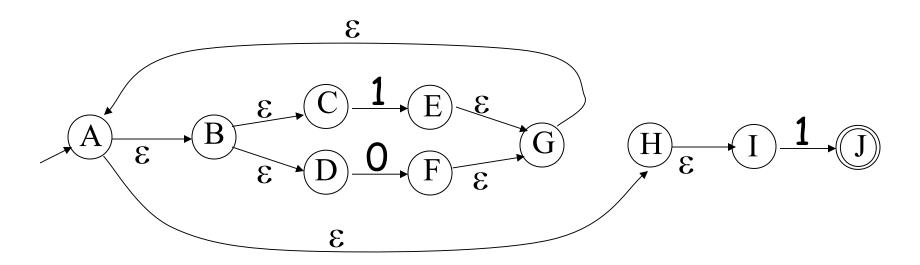


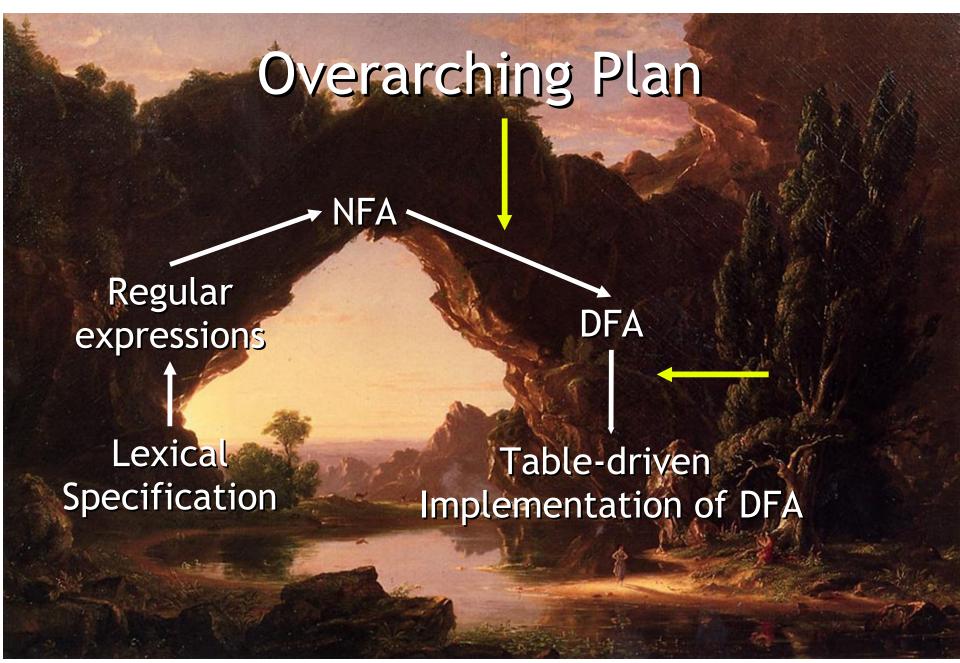
Example of RegExp -> NFA Conversion

Consider the regular expression

$$(1 | 0)* 1$$

The NFA is

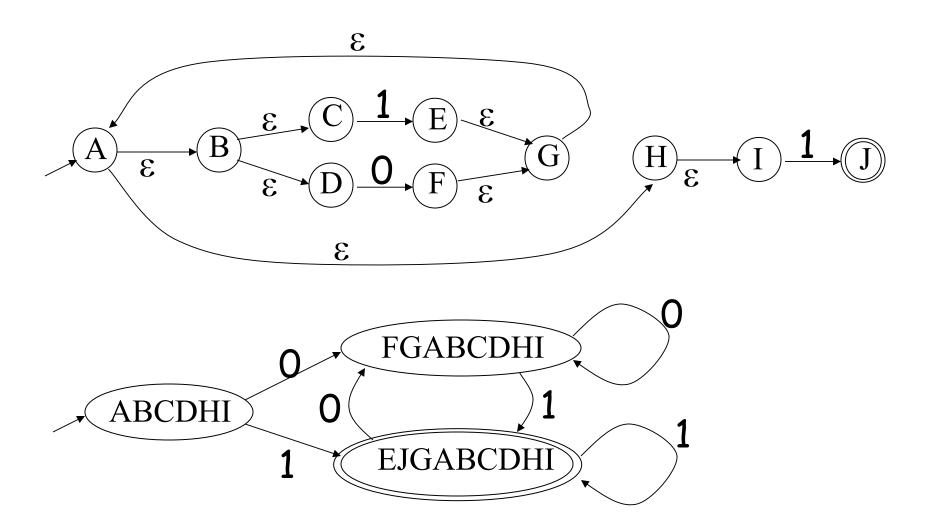




NFA to DFA: The Trick

- Simulate the NFA
- Each state of DFA
 - = a non-empty *subset of states* of the NFA
- Start state
 - = the set of NFA states reachable through ε-moves from NFA start state
- Add a transition $S \rightarrow a S'$ to DFA iff
 - S' is the set of NFA states reachable from the states in S after seeing the input a
 - considering ε-moves as well

NFA → DFA Example



NFA → DFA: Remark

An NFA may be in many states at any time

How many different states?

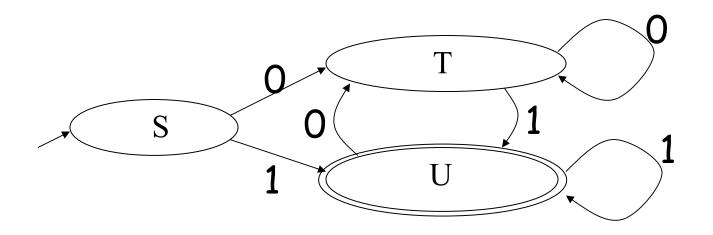
 If there are N states, the NFA must be in some subset of those N states

- How many non-empty subsets are there?
 - 2^N 1 = finitely many

Implementation

- A DFA can be implemented by a 2D table T
 - One dimension is "states"
 - Other dimension is "input symbols"
 - For every transition $S_i \rightarrow a S_k$ define T[i,a] = k
- DFA "execution"
 - If in state S_i and input a, read T[i,a] = k and skip to state S_k
 - Very efficient

Table Implementation of a DFA



	0	1
S	Τ	U
Η	Τ	U
J	Τ	U

Implementation (Cont.)

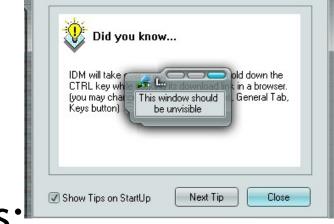
 NFA → DFA conversion is at the heart of tools such as flex or ocamllex

But, DFAs can be huge

 In practice, flex-like tools trade off speed for space in the choice of NFA and DFA representations

PA2: Lexical Analysis

- Correctness is job #1.
 - And job #2 and #3!

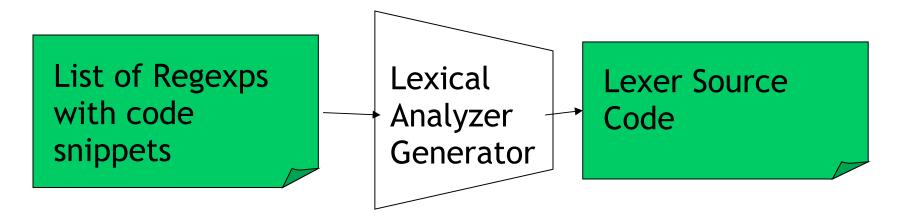


Tip of the Day

- Tips on building large systems:
 - Keep it simple
 - Design systems that can be tested
 - Don't optimize prematurely
 - It is easier to modify a working system than to get a system working

Lexical Analyzer Generator

- Tools like lex and flex and ocamllex will build lexers for you!
- You will use this for PA2



- I'll explain ocamllex; others are similar
 - See PA2 documentation

Ocamllex "lexer.mll" file

```
(* raw preamble code
      type declarations, utility functions, etc. *)
let re_name; = re;
rule normal_tokens = parse
  re<sub>1</sub> { token<sub>1</sub> }
  re, { token, }
and special, okens = parse
  re<sub>n</sub> { token<sub>n</sub> }
```

Example "lexer.mll"

```
type token = Tok_Integer of int
                                        (* 123 *)
                                        (* / *)
       | Tok_Divide
let digit = ['0' - '9']
rule initial = parse
             { Tok_Divide }
| digit digit* { let token_string = Lexing.lexeme lexbuf in
              let token_val = int_of_string token_string in
              Tok_Integer(token_val) }
             { Printf.printf "Error!\n"; exit 1 }
```

Adding Winged Comments

```
type token = Tok_Integer of int
                                     (* 123 *)
        | Tok_Divide
let digit = ['0' - '9']
rule initial = parse
  "//" { eol_comment }
             { Tok_Divide }
 digit digit* { let token_string = Lexing.lexeme lexbuf in
                let token_val = int_of_string token_string in
                Tok_Integer(token_val) }
               { Printf.printf "Error!\n"; exit 1 }
and eol_comment = parse
 '\n' { initial lexbuf }
      { eol_comment lexbuf }
```

Using Lexical Analyzer Generators

\$ ocamllex lexer.mll

```
45 states, 1083 transitions, table size 4602 bytes
(* your main.ml file ... *)
let file_input = open_in "file.cl" in
let lexbuf = Lexing.from_channel file_input in
let token = Lexer.initial lexbuf in
match token with
| Tok_Divide -> printf "Divide Token!\n"
| Tok_Integer(x) -> printf "Integer Token = %d\n" x
```

How Big Is PA2?

- The reference "lexer.mll" file is 88 lines
 - Perhaps another 20 lines to keep track of input line numbers
 - Perhaps another 20 lines to open the file and get a list of tokens
 - Then 65 lines to serialize the output
 - I'm sure it's possible to be smaller!

Conclusion:

 This isn't a code slog, it's about careful forethought and precision.

Warning!

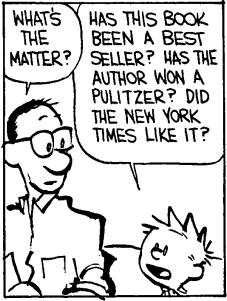
- You may be tempted to use OCaml for PA2 based on that demo.
- However, you probably want to save OCaml for one of the harder assignments later.

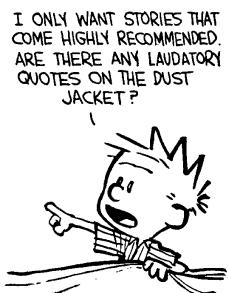


Test Yourself! Exam Practice.

- Are practical parsers and scanners based on deterministic or non-deterministic automata?
- How can regular expressions be used to specify nested constructs?
- How is a two-dimensional transition table used in tabledriven scanning?









Homework

- PA1 due
- Textbook Reading, CD Reading